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Thermal-noise-limited underground interferometer CLIO

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Abstract
We report on the current status of CLIO (Cryogenic Laser Interferometer Observatory), which is a prototype interferometer for LCGT (large scale cryogenic gravitational-wave telescope). LCGT is a Japanese next-generation interferometric gravitational-wave detector featuring the use of cryogenic mirrors and a quiet underground site. The main purpose of CLIO is to demonstrate a reduction of the mirror thermal noise by cooling the sapphire mirrors. CLIO is located in an underground site of the Kamioka mine, 1000 m deep from the mountain top, to verify its advantages. After a few years of commissioning work, we have achieved a thermal-noise-limited sensitivity at room temperature. One of the main results of noise hunting was the elimination of thermal noise caused by a conductive coil holder coupled with a pendulum through magnets.

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(Some figures in this article are in colour only in the electronic version)
1. Introduction

CLIO (Cryogenic Laser Interferometer Observatory) [1–4] is a prototype for the next Japanese gravitational wave (GW) telescope project, LCGT (large scale cryogenic gravitational-wave telescope) [5], featuring the use of cryogenic mirrors and a quiet underground site. The main goal of CLIO is to demonstrate an improvement of sensitivity through a reduction of mirror thermal noise by cooling the sapphire mirrors. The design sensitivity is limited by the mirror thermal noise and the suspension thermal noise around 100 Hz, which will be reduced after cooling. Through works on noise hunting, we achieved a thermal-noise-limited sensitivity at room temperature. One of the main factors concerning the sensitivity improvement was to remove thermal noise due to a conductive coil holder coupled with a pendulum through magnets. Firstly, we report on the best displacement sensitivity we have achieved and noise hunting in recent works. Next, we focus on the verification of the thermal noise due to the coil holder by theory and an experiment.

2. Thermal-noise-limited sensitivity

2.1. Configuration of CLIO

CLIO is located in Kamioka mine, which is 220 km from Tokyo, and lies 1000 m underground from the top of a mountain. LCGT is planned to be constructed in this area. This underground site is suitable for interferometric GW detectors because the seismic noise is less than that in an urban area by about two orders [6, 7]. This merit is helpful to achieve the target sensitivity and to obtain stability. Owing to this advantage of low frequency, observations for the Vela pulsar were performed in 2007 [8].

Figure 1 shows a schematic view of CLIO. A laser beam (Innolight Inc. Mephisto) has a power of 2 W and a 1064 nm wavelength. It is shaped into TEM00 through a mode cleaner (MC) cavity with a length of 9.5 m, and then injected to two 100 m length FP cavities after being divided by a beam splitter. These cavities are arranged in an L-shape. All of the returned (reflected) beam from each arm cavity is extracted by an optical circulator formed by a λ/4 plate and a polarized beam splitter. Thus, this configuration employs neither optical recombination by a Michelson interferometer nor optical recycling schemes. The cavities are kept on resonance, called locked, by servo systems. The Pound–Drever–Hall technique [9] is employed as a readout method for displacement signals of the mirrors. For that purpose, the phase modulations at 15.8 MHz and 11.97 MHz are used for the arm cavities and the mode cleaner cavity, respectively. A multistage control system [10] is applied for laser frequency stabilization, which has two cascaded loops of the MC and an arm cavity. The inline arm is locked by controlling the frequency. The perpendicular arm is locked by controlling the mirror. A differential displacement between two arm cavities, which corresponds to GW signals, can be obtained from a feedback signal to the coil-magnet actuators.

The four mirrors of the two arm cavities are individually suspended by six-stage pendulums, which include four-stage blade springs and two-stage wire suspensions for isolation from any seismic vibration. The mirrors have weights of 1.8 kg (end) and 1.9 kg (front), made of sapphire. They are suspended by bolfur6 wires at the last stage, whose resonant frequency is 0.79 Hz. The pendulum has a resonant frequency of a primary mode of about 0.5 Hz. The angular alignments of all mirrors are tuned by movable stages on the suspensions. Coil-magnet actuators are set for the front mirror in the perpendicular cavity only, so as to keep the optical path length of the cavity locked.

6 A product of UNITICA http://www.unitika.co.jp/.
Until now, cryogenic systems have been developed [11–13] and progressed [14]. Thus, cooling mirrors were realized [15]. All sapphire mirrors were cooled down to the required temperature of under 20 K. However, thermal noise due to a conductive coil holder, which appeared from 20 Hz to 300 Hz with a slope of $f^{-2}$ (f was the frequency) prevented the sensitivity from reaching the thermal noises of suspensions and mirrors, at both room temperature and the cool temperature [15]. We could remove the extra thermal noise by noise hunting in recent works, and reached the design sensitivity at room temperature.

2.2. Progress of noise hunting

CLIO displacement noise reached the predicted thermal noise levels. Figure 2 shows the improvement of the displacement noise in 2008. The current best-floor sensitivity is $2.5 \times 10^{-19}$ m Hz$^{-1/2}$ at 250 Hz. In the frequency region of 20–80 Hz, the spectrum is close to the suspension thermal noise, which comes from wire-material dissipations of the structure damping (the internal damping [16]). The theoretical prediction was calculated using the quality factor of a pendulum of $10^5$, which was estimated from the measured violin $Q$. The mirror thermal noise is also close to the sensitivity and estimated from the bulk thermal noise of the thermoelastic damping. Details of this progress and estimations will be described in an independent paper [17].

The noise hunting of the CLIO interferometer has progressed at room temperature. The improvement of the broad region from 20 Hz to 300 Hz came mainly from avoiding a kind

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**Figure 1.** Schematic view of CLIO; CLIO is a so-called locked Fabry–Perot interferometer, which has two 100 m Fabry–Perot cavities with a mode cleaner. The optics, like the lenses, the Faraday-isolators and some wave plates are omitted in this figure. EOM, electro-optic modulator; HWP, half-wave plate; QWP, quarter-wave plate; MMT, mode matching telescope; PBS, polarized beam splitter.
of pendulum thermal noise due to eddy currents in a coil holder induced by magnets glued onto the mirror. A beam centering adjustment also reduced noisy structures in this region. By adjusting the beam centering, we could reduce the length fluctuation of the cavities coupled with a mirror-angle fluctuation. In the high-frequency region, repairing the servo-circuits malfunction contributed to the reach of the shot noise. Using thinner suspension wires made of bolfur, whose diameters were changed from 0.1 mm to 0.05 mm, shifted the violin modes to higher frequencies, so as to separate the skirts of violin modes from the mirror thermal noise region. One reason for the improvement at around 10 Hz was the removal of magnets on the upper mass for extended actuation, which had been shaken by damping magnets.

The greatest contributing factor for improving the sensitivity was to identify the pendulum thermal noise due to a coil holder with a slope of $f^{-2}$. Let us emphasize that this is not the suspension thermal noise. The design sensitivity was calculated to be limited by the suspension thermal noise with a slope of $f^{-5/2}$, which comes from wire-material dissipations of the internal damping [16]. On the other hand, the thermal noise due to a coil holder was caused by mechanical losses by eddy currents in the conductive coil holder coupled with a pendulum. The details are explained in the next section.

3. Thermal noise due to a coil holder

3.1. Theoretical estimation

Pendulum thermal fluctuation is caused by several kinds of dissipations coupled with the whole pendulum. There are studies of those dissipations: an internal loss in the materials of
suspension wires [16, 18], clamps of wires [19], residual air [20], coil-magnet actuators [21] and a reference mass with coils [22, 23]. The pendulum thermal noise due to the reference mass with coils (the coil holder in our case) is the most interesting in this section. An oscillation of the pendulum gives rise to eddy currents by electromagnetic induction in the coil holder. These currents generate Joule heat in the material of the coil holder. According to the fluctuation–dissipation theorem (FDT) [24], the dissipation of the Joule heat causes a thermal fluctuation of the pendulum through coupling with magnets glued onto the mirror.

A quality factor of the pendulum, caused by the losses of conductive materials (reference masses) near the magnets, was derived [22] as

\[
Q = \frac{m\omega_0}{2\pi \sigma \left( \frac{3\mu_0 M}{4\pi} \right)^2 J},
\]

which was verified by not only Cagnoli [22] but also Frasca [23]. Here, \(\omega_0 = 2\pi f_0\), \(f_0\) is the pendulum frequency, \(m\) the mirror mass, \(\sigma\) the median conductivity of the materials, \(\mu_0\) the permeability, \(M\) the magnetic dipole moment of the magnet and \(J\) a geometrical factor that depends on the shape of the conductor, given by

\[
J = \int_{z_1}^{z_2} \int_{r_1}^{r_2} \frac{r^2 z^2}{(r^2 + z^2)^{5/2}} dr dz.
\]

Here, the conductor is assumed to have a center-holed cylindrical shape with an inner radius \(r_1\), outer radius \(r_2\) and length \(z_2 - z_1\) for simplicity. The center of the magnet is placed at \(z = 0\), and the length from the magnet to the edge of a conductor is \(z_1\). The cause of thermal fluctuation is dissipation of the viscous damping, whose loss angle is \(\phi = \omega/\omega_0 Q\), due to eddy currents in the conductor. By using the FDT and applying the \(Q\)-factor of equation (1), the thermal fluctuation of a pendulum (a harmonic oscillator) in a higher off-resonant region is approximately written as

\[
G = \frac{4k_B T N}{m^2 \omega^4} 2\pi \sigma \left( \frac{3\mu_0 M}{4\pi} \right)^2 J,
\]

where \(\sqrt{G}\) is a one-sided power spectrum density, \(k_B\) the Boltzmann constant and \(T\) the temperature of the conductors and the pendulum. \(N\) is the pair number of a magnet and a conductor that has a homogeneous shape around each magnet.

In order to estimate the thermal noise due to the coil holder by equation (3) and the \(Q\)-factor of pendulum by equation (1), the magnetic dipole moment, \(M\), needs to be known. However, the magnetic moment is not usually easy to measure. It is practicable to utilize a coil magnet actuator coupling so as to estimate the magnetic moment. By using one coil magnet actuator, the force of \(F = \alpha I\) can be applied for the test mass. The coupling factor, \(\alpha\), is the conversion efficiency between the current, \(I\), in a coil circuit and the force, \(F\). This coupling factor is related to the magnetic moment of a magnet by

\[
\alpha = \frac{3\mu_0 M}{2} \sum_{z=0}^{w-1} \sum_{n=0}^{u-1} \frac{(z_1 + dn)(r_1 + ds)^2}{((z_1 + dn)^2 + (r_1 + ds)^2)^{5/2}}.
\]

Here, the solenoidal coil, which consists of a conductive wire with a diameter of \(d\), is wound around a bobbin with a radius of \(r_1 - d/2\). We approximately regarded the coil as a bunch of rings for modeling, as shown in figure 3. On the heels of the first ring at a distance of \(z = z_1\) from the magnet, rings of \(w\) turns are lined by a gap of \(d\) side by side \((z = z_1 + dn; n = 0, 1, 2, \ldots, w - 1)\). When the coil is folded like layers to outside of its radius direction, it can be regarded as \(r = r_1 + ds; s = 0, 1, 2, \ldots, u - 1\) using a folding number of \(u\). By measuring \(\alpha\), we can estimate the magnetic dipole moment, \(M\), using
equation (4). The coupling factor per one coil-magnet actuator, $\alpha$, is yielded from the relation $\alpha = A_{100}R_c m (2\pi \times 100)^2/N_c$. $A_{100}$ is the measured actuator response at 100 Hz, which is a transfer function from the driver input voltage to the mirror displacement. This response at the front mirror is measured using a Michelson interferometer constructed with front mirrors and the BS. $R_c$ ($R_c = 50 \Omega$ in CLIO) is the resistance of volt-current conversion in the coil driver and $m$ is the weight of a test mass ($m = 1.9$ kg at the front mirror in CLIO). $N_c$ ($N_c = 4$) is the pair number of a magnet and a coil.

The sensitivity of CLIO was improved by replacing a coil holder. We tried to prove that the noise floor with the previous coil holder came from the above thermal noise. However, the spectrum before noise hunting included some other noises. In order to take the other noises into account, an intermediate spectrum before the best sensitivity in figure 2 was used as a background (BG) noise without eddy currents. Figure 4 shows a comparison between the measured spectrum before replacing the coil holder and the calculation from equation (3). The noise floor was almost matched with the calculation from 20 Hz to 200 Hz. The parameters for the estimates are indicated in table 1. The spectrum of the ‘new coil-holder’ in figure 4 is employed as the BG noise owing to the first measurement using the new coil holder, which is close to the BG noise of the ‘before noise hunting’. For simplicity, we regarded a spectrum of the ‘new coil holder’ from 20 Hz to 100 Hz as the ‘BG model’ with a slope of $f^{-5/2}$ by fit-by-eye. The sensitivity in a high frequency region of figure 4 was improved because the servo-circuit had been already mended. The spectrum of the ‘new coil holder’ includes some changes, not only to the coil holder but also to other interferometer settings. Therefore a special experiment, which replaces only the coil holder, is described in section 3.2.

The evaluation did not perfectly agree with the measured spectrum in figure 4. One reason is a limitation of the coil holder modeling. The estimated geometrical factor, $J$, is more uncertain than the other parameters, because the previous coil holder had a cubic shaped structure around a coil in spite of the calculation limited by the cylindrical shape from equation (2). A picture of this coil holder is shown in figure 6. We estimated $J$ to be a band line that has a lower limit of $J = 5600$ and an upper limit of $J = 9800$. $J$ of 5600 is the lower limit and an underestimate because it does not include the volume of the cubic corner beyond the cylindrical shape with $r_2$ of 15 mm. $J$ of 9000 is an approximation of the whole cubic, which corresponds to $r_2$ of a length from the center of the coil to a diagonal corner (21 mm). The upper limit is calculated as $J = 9800$ by adding the effect of the outer frame (beyond the cubic around the coil) assuming a plate ($r_1 = 21$ mm, $r_2 = 32$ mm, $z_1 = 10$ mm and $z_2 = 20$ mm), which is rather an overestimate since the actual outer frame is not
Figure 4. Comparison between the measured spectrum and a theoretical calculation of the thermal noise due to the coil holder. The solid lines of blue and gray indicate measured spectra with the previous coil holder configuration and with the new coil holder configuration, respectively. The dashed line denotes a background (BG) model as part of the sensitivity with the new coil holder. The orange band is the sum of the theoretical calculation of the thermal noise due to the coil holder material ($J$ of equation (2): from 5600 to 9800) and the BG model.

Figure 5. Improvement of the sensitivity by replacing the coil holder. The coil holder made of aluminum was replaced with diflon bobbins, which were an electrical isolator.

a plate shape. Numerical simulation is needed for more precise estimation using $J$ of the coil holder with a complex shape. Another reason is an error of the measured $\alpha$, which is about 10%. The other reason is most likely a difference of BG noise in the region from 20 Hz to 50 Hz. In the ‘before noise hunting’, it is possible to inject the seismic noise via the coil holder
Table 1. Parameters $\alpha$ and $M$ are the average of all magnets. $r_2$ at the previous coil holder indicates the length from the center of the coil to a side or to a diagonal corner. The $J$ values were calculated from $r_2$ of two patterns (and the outer frame).

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Previous coil holder</th>
<th>New coil holder</th>
</tr>
</thead>
<tbody>
<tr>
<td>Coil-holder (bobbin)</td>
<td>Al</td>
<td>Macor</td>
</tr>
<tr>
<td>$\sigma$ ($\Omega^{-1}$m$^{-1}$)</td>
<td>$3.6 \times 10^7$</td>
<td>$10^{-13}$</td>
</tr>
<tr>
<td>$r_1$ (mm)</td>
<td>12</td>
<td>–</td>
</tr>
<tr>
<td>$r_2$ (mm)</td>
<td>$15 - 21$</td>
<td>–</td>
</tr>
<tr>
<td>$z_1$ (mm)</td>
<td>0</td>
<td>–</td>
</tr>
<tr>
<td>$z_2$ (mm)</td>
<td>20</td>
<td>–</td>
</tr>
<tr>
<td>Magnet</td>
<td>Nd-Fe-B</td>
<td>Sm-Co</td>
</tr>
<tr>
<td>Magnet size</td>
<td>$\phi 2 \text{ mm} \times 10 \text{ mm}$</td>
<td>$\phi 1 \text{ mm} \times 10 \text{ mm}$</td>
</tr>
<tr>
<td>$\alpha$ ($\text{NA}^{-1}$)</td>
<td>$3.6 \times 10^{-3}$</td>
<td>$4.8 \times 10^{-4}$</td>
</tr>
<tr>
<td>Estimated value $M$ (J T$^{-1}$)</td>
<td>0.0165</td>
<td>0.0034</td>
</tr>
<tr>
<td>$J$ (m$^{-3}$)</td>
<td>5600–9000 (9800)</td>
<td>–</td>
</tr>
<tr>
<td>$Q_{\text{holder}}$</td>
<td>$4.6 \times 10^4$</td>
<td>–</td>
</tr>
<tr>
<td>$\sqrt{G_{\text{holder}}} \text{ at } 100 \text{ Hz} (\text{m Hz}^{-1/2})$</td>
<td>$2.5 \times 10^{-18}$</td>
<td>–</td>
</tr>
</tbody>
</table>

fixed on an optical stage or inject angular fluctuations of mirrors via an imperfection of beam centering as mentioned in section 2.2.

3.2. Experimental verification

We tested whether the sensitivity could be improved by replacing the coil holder with an electrical isolator. Figure 5 shows the result of that experiment. The sensitivity was improved by replacing the coil holder. The settings of the CLIO interferometer were not changed in the test, except for the coil holder. That is why the noise floor with the previous coil holder can be regarded as being the thermal noise due to the coil holder coupled with the pendulum. In this experiment, diflon bobbins (not the ‘new coil holder’ in table 1 and figure 4) were employed so as to suppress eddy currents. The spectrum of the diflon bobbin was not employed as the BG noise in figure 4 because the bobbin was supported by aluminum plates with a complex shape, which did not perfectly suppress eddy currents. The aluminum was used as the material of the previous coil holder for reasons of cryogenic compatibility as good thermal conduction. Further, a precise and quantitative identification of the pendulum thermal fluctuation due to viscous damping was performed using coil magnet actuators [21].

3.3. Solution

The coil holder was redesigned so that the pendulum could sufficiently avoid mechanical losses due to eddy currents in the coil holder. The new coil holder at room temperature is shown
Figure 6. Photographs of coil holders. Left: the previous coil holder. Coils are surrounded by a coil holder made of aluminum, and fixed into the coil holder using stycast. Right: the new coil holder. Coils are wound on macor bobbins fixed on an aluminum frame through diflon holders.

Coil bobbins are made of a macor (ceramic), which has an electrical conductivity of $10^{-13} \, \Omega^{-1} \, m^{-1}$. The aluminum frame is separated from the magnets. The magnets were also changed from 2 mm to 1 mm in diameter, so that their magnetic moment could be reduced, and the material changed from Nd-Fe-B to Sm-Co as a precaution against Barkhausen noise. The current best sensitivity at room temperature as shown in figure 2 was achieved with this coil holder configuration.

For cryogenic compatibility, the macor bobbins were replaced with aluminum nitride bobbins, which is an electrical isolator with thermal conductivity.

4. Summary

CLIO is a prototype interferometer for LCGT, which is located in an underground site of the Kamioka mine. After a few years of commissioning work, we achieved a thermal-noise-limited sensitivity at room temperature. The predicted suspension thermal noise and the mirror thermal noise were very close to the measured sensitivity. The main factor concerning the sensitivity improvement was to remove thermal noise due to a conductive coil holder coupled with a pendulum through magnets. The experimental result was supported by the theoretical estimation. This result became a direct verification in a noise spectrum of the estimation by Cagnoli and Frasca. We are ready to proceed to the cryogenic experiment, which is the main goal of thermal noise reduction in CLIO. Currently, we are preparing to cool the mirrors as the next step.

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