Suppression of nonadiabatic losses of molecules from chip-based microtraps

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Polar molecules in selected quantum states can be guided, decelerated, and trapped using electric fields created by microstructured electrodes on a chip. Here we explore how nonadiabatic transitions between levels in which the molecules are trapped and levels in which the molecules are not trapped can be suppressed. We use 12CO and 13CO (\(a^1\Pi_1, v = 0\)) molecules, prepared in the upper \(\Lambda\)-doublet component of the \(J = 1\) rotational level, and study the trap loss as a function of an offset magnetic field. The experimentally observed suppression (enhancement) of the nonadiabatic transitions for 13CO (12CO) with increasing magnetic field is quantitatively explained.

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I. INTRODUCTION

The manipulation and control of polar molecules above a chip using electric fields produced by microstructured electrodes on the chip surface is a fascinating new research field [1]. Miniaturization of the electric-field structures enables the creation of large field gradients, that is, large forces and tight potential wells for polar molecules. A fundamental assumption that is made when considering the force imposed on the molecules is that their potential energy only depends on the electric-field strength. This is usually a good assumption, since the molecules will reorient themselves and follow the new quantization axis when the field changes direction and their potential energy will change smoothly when the strength of the field changes. This approximation can break down, however, when the quantum state that is used for manipulation couples to another quantum state that is very close in energy. If the energy of the quantum state changes at a rate that is fast compared to the energetic splitting, transitions between these states are likely to occur. For trapped molecules in so-called low-field-seeking states in a static electric potential, such transitions are particularly disastrous when they end up in high-field-seeking states or in states that are only weakly influenced by the electric fields, as this results in a loss of the molecules from the trap. This effect has been investigated previously for ammonia molecules in a Ioffe-Pritchard type electrostatic trap with a variable field minimum. In this macroscopic electrostatic trap, losses due to nonadiabatic transitions were observed on a second time scale when the electric field at the center of the trap was zero; with a nonzero electric-field minimum at the center of the trap, these losses could be avoided [2]. Nonadiabatic transitions have recently also been investigated in a “conventional,” that is, macroscopic, Stark decelerator in which electric fields are rapidly switched between two different configurations. There, these transitions have been found to lead to significant losses of molecules when they are in low electric fields [3]. Similar trap losses will be much more pronounced on a microchip, where the length scales are much shorter and where the electric-field vectors change much faster. For atoms in a three-dimensional magnetic quadrupole trap, the trap losses due to spin flip (or Majorana) transitions have been shown to be inversely proportional to the square of the diameter of the atom cloud [4]. On atom chips, where paramagnetic atoms are manipulated above a surface using magnetic fields produced by current-carrying wires, trap losses due to Majorana transitions are therefore well known but can be conveniently prevented by using an offset magnetic field [5]. Due to the geometry of the molecule chip, however, applying a static offset electric field is not possible, and other solutions must be sought.

We have recently demonstrated that metastable CO molecules, laser-prepared in the upper \(\Lambda\)-doublet component of the \(J = 1\) level of the \(a^1\Pi_1, v = 0\) state can be guided, decelerated, and trapped on a chip. In these experiments, nonadiabatic losses have been observed for 13C16O. In this most abundant carbon monoxide isotopologue, the level that is low-field-seeking becomes degenerate with a level that is only weakly influenced by an electric field when the electric-field strength goes to zero. Every time that the trapped molecules pass near the zero-field region at the center of a microtrap, they can make a transition between these levels and thereby be lost from the trap. This degeneracy is lifted in 13C16O due to the hyperfine splitting (the 13C nucleus has a nuclear spin \(I = 1/2\)), and the low-field-seeking levels never come closer than 50 MHz to the nontrappable levels. Therefore, changing from 12C16O to 13C16O (referred to as 12CO and 13CO from now on) in the experiment greatly improves the efficiency with which the molecules can be guided and decelerated over the surface and enables trapping of the latter molecules in stationary traps on the chip [1].

Although it is evident that the 50-MHz splitting between the low-field-seeking and nontrappable levels in 13CO is beneficial, it is not \textit{a priori} clear whether a smaller splitting would already be sufficient or if a still larger splitting would actually be needed to prevent all losses. While the hyperfine splitting in 13CO cannot be varied, the degeneracy can be lifted by a variable amount in the normal 12CO isotopologue by using a magnetic field. If a magnetic field is applied in addition to the electric field, a splitting can be induced between the low-field-seeking and nontrappable levels of 12CO that depends on the strength of the applied magnetic field; in 13CO, a magnetic field will actually decrease the splitting between the low-field-seeking and nontrappable levels.
In this paper, we present measurements of the efficiency with which CO molecules are transported over the chip—while they are confined in electric-field minima that are traveling at a constant velocity—as a function of magnetic-field strength. It is observed that, in the case of $^{12}$CO, the losses due to nonadiabatic transitions can be completely suppressed in sufficiently high magnetic fields; for $^{13}$CO, on the other hand, the trap losses increase with increasing magnetic field. A theoretical model that can quantitatively explain these observations is also presented. Although the chip is ultimately used to decelerate molecules to a standstill, measuring the efficiency with which molecules are guided at a constant velocity provides a detailed insight into the underlying trap-loss mechanism. Limiting the experiments to constant velocity guiding also makes them more tractable: bringing molecules to a standstill and subsequently detecting them has thus far required five separate phases of acceleration, which greatly complicates efforts to understand the details of the loss mechanism using numerical calculations [1]. While deceleration at a constant rate to a nonzero final velocity is possible, the measurable signal in such experiments is significantly lower than in constant velocity guiding. Despite the fact that we only measure at constant velocity, we nonetheless apply the model to examine the nonadiabatic losses expected during deceleration. This work thereby furthers the goal of extending trapping on the molecule chip to a wider range of molecules.

II. EXPERIMENTAL SETUP

A scheme of the experimental setup is shown in Fig. 1. A mixture of 20% CO in krypton is expanded into vacuum from a pulsed valve (General Valve, Series 99), cooled to a temperature of 140 K. In this way, a molecular beam with a mean velocity of 300 m/s and with a full-width-half-maximum spread of the velocity distribution of approximately 50 m/s is produced. This beam passes through two 1-mm-diameter skimmers and two differential pumping stages (the valve and first skimmer are not shown in the figure) before entering the chamber in which the molecule chip is mounted. Just in front of the second skimmer, the ground-state CO molecules are excited to the upper $\Delta$-doublet component of the $J = 1$ level of the metastable $a^3\Pi_1$, $v = 0$ state, using narrow-band pulsed laser radiation around 206 nm (1 mJ in a 5-ns pulse with a bandwidth of about 150 MHz). The metastable CO molecules are subsequently guided in traveling potential wells that move at a constant speed of 300 m/s parallel to the surface of the molecule chip. A uniform magnetic field is applied to the region around the chip using a pair of 30-cm-diameter planar coils separated by 23 cm (not shown in the figure). The coils are oriented such that the magnetic field is parallel to the long axis of the chip electrodes, that is, along the $z$ axis, ensuring that the magnetic field is always perpendicular to the electric field (vide infra). The CO molecules that have been stably transported over the chip will pass through the 50-µm-high exit slit and enter the ionization detection region a short distance further downstream. There, the metastable CO molecules are resonantly excited to selected rotational levels in the $b^3\Sigma^+$, $v' = 0$ state using pulsed laser radiation at 283 nm (4 mJ in a 5-ns pulse with a 0.2-cm$^{-1}$ bandwidth). A second photon from the same laser ionizes the molecules and the parent ions are mass-selectively detected in a compact linear time-of-flight setup using a microchannel plate (MCP) detector. This detection scheme has been implemented in addition to the Auger detection scheme that we have used in earlier studies [1,6,7] as it is more versatile and can also be applied to detect other molecules. In addition, the detection sensitivity of the ion detector is less affected by the magnetic field than that of the Auger detector.

The molecule chip and its operation principle have been described in detail before [6,7], and only the features that are essential for understanding of the present experiment are discussed here. The active area of the chip consists of an array of 1254 equidistant electrodes, each 10 µm wide and 4 mm long, with a center-to-center distance of 40 µm. An edge-on view of the chip electrodes (with the 4-mm dimension of the electrodes perpendicular to plane of the figure) is shown in Fig. 2. The potential (in volts) applied to an electrode at a given moment in time is indicated directly above the electrode; these six potentials are repeated periodically on the electrodes on either side of those drawn here. Because the electrodes are much longer than the period length of the array, the electric-field distribution can be regarded as two-dimensional; that is, the component of the electric field along the $z$ axis can be neglected. This is of importance for the present experiments, because only in this case the applied magnetic field is always perpendicular to the electric field. The calculated contour lines of equal electric-field strength in the free space above the chip show electric-field minima that are separated by 120 µm; that is, there are two electric-field minima per period, centered about 25 µm above the surface of the chip. By applying sinusoidal waveforms with a frequency $\nu$ to the electrodes, these minima can be translated parallel to the surface with a speed given by $v = 120 \mu m \cdot \nu$. When these waveforms are perfectly harmonic and have the correct amplitude, offset, and phase, the minima move with a constant velocity at a constant height above the surface, and the shape of the field-strength distribution does not change in time. Because
an electric-field-strength minimum acts as a trap for molecules in low-field-seeking states, these fields act as tubular moving traps that can be used to guide the molecules over the surface of the chip. The tubular traps are closed at the end by the fringe fields caused by the neighboring electrodes. Near the ends of the about 4-mm-long traps, the electric field will necessarily have a component along the $z$ axis, that is, parallel to the applied magnetic field. In the present study, where the molecules are guided at 300 m/s over the chip and are therefore on the chip for less than 200 $\mu$s, these end effects are neglected.

The region near an electric-field-strength minimum at $(x, y) = (x_0, y_0)$ is a quadrupole, with an electric potential given by

$$V = \frac{\alpha}{2} r^2 \cos(2\phi - \phi_0),$$

(1)

where $x - x_0 = r \cos \phi$ and $y - y_0 = r \sin \phi$. In the current experiment, sinusoidal waveforms with an amplitude of 180 V are applied to the electrodes, yielding a value of $\alpha = 0.054$ V/µm² [7]. The resulting electric field is given by

$$\vec{E} = -\alpha r [\cos(\phi_0 - \phi)\hat{x} + \sin(\phi_0 - \phi)\hat{y}].$$

(2)

The strength of the electric field, $|\vec{E}| = \alpha r$, depends only on the $r$ coordinate, but the direction of the field vector, $\phi' = \phi_0 - \phi + \pi$, depends on the coordinate $\phi$ and on the phase factor $\phi_0$. While the direction of the field vector changes as a result of the motion of the molecule in the quadrupole field (and thus changing $\phi$), the direction of the field at any given position relative to the minimum also rotates when the minimum is translated over the chip. It is seen from the electric-field vectors shown in the insets of Fig. 2 that the frequency of this rotation is 1.5 times the frequency of the applied waveforms and that the direction of the rotation is clockwise; that is, the rotation vector points along the positive $z$ axis and $\phi_0$ increases linearly in time. To guide the molecules over the chip at 300 m/s, harmonic waveforms with a frequency $\nu$ of 2.5 MHz must be applied, resulting in a rotation frequency of 3.75 MHz.

For CO molecules in the low-field-seeking component of the $J = 1$ level, the depth of the tubular traps above the chip is about 60 mK. This implies that CO molecules with a speed of up to 6 m/s relative to the center of the trap can be captured. The oscillation frequency of the molecules in the radial direction of the tubular traps is in the 100- to 250-kHz range. These parameters are of importance for the nonadiabatic transitions as these determine with which velocity and how often per second the CO molecules pass by the zero-field region of the traps.

It turns out that, in the actual experiment, the tubular traps do not move perfectly smoothly over the chip. Due to imperfections in the amplitude, offset, and phase of the waveforms that we have used, the tubular traps are jittering at rather high velocities. The motion of the center of the traps relative to the ideal, constant velocity motion can be calculated by measuring the real waveforms applied to the chip and using these to compute the position of the minimum for each point in time. The top row of Fig. 3 shows the motion of a minimum when the waveforms that we refer to as the “standard waveforms” have been used. The range of this motion extends over $\pm 2 \mu$m in the $x$ and $y$ coordinates. Although this is considerably smaller than the size of the trapping region, this...
motionsignificantlyenlargestheeffective regionin which nonadiabatic transitions can occur. Moreover, the entire path is tracedout periodically every $T = 2/\nu = 800 \text{ ns}$; because the motion occurs on such a short timescal e, the speed with which the trap center moves, and therefore the relat ivespeed with which the molecules encounter the trap center, can be as high as 100 m/s. T o improve the waveform s, we inserted an LC filter in the output stage of the amplifiers, thereby reducingthe harmonic distortion. The resultingmotion using these “improved waveforms” is shown in thebottom row of Fig. 3. It is seen that not only the range of the motion is nowcontracted but also the speed with which the trap centerjitters is reduced by about a factor of two.

III. THEORETICAL MODEL

A. Eigenenergies in combined fields

In order to describe the nonadiabatic transitions in CO, we must first derive the energy levels of CO in combined electric and magnetic fields. For this, the field-free Hamiltonian is expanded with Stark and Zeeman contributions; that is,

$$\hat{H} = \hat{H}_{\text{A,bfs}} + \hat{H}_{\text{S}} + \hat{H}_{Z}. \tag{3}$$

Here, $\hat{H}_{\text{A,bfs}}$ describes the $\Lambda$ doubling of the $a^3\Pi_1$, $\nu = 0$, $J = 1$ level for either $^{12}\text{CO}$ or $^{13}\text{CO}$ and also includes the hyperfine splitting of each $\Lambda$ component into $F = 1/2$ and $F = 3/2$ hyperfine sublevels for $^{13}\text{CO}$; $\hat{H}_{\text{S}} = -\mu_E \cdot \vec{E}$ is the Stark interaction Hamiltonian and $\hat{H}_{Z} = -\mu_B \cdot \vec{B}$ is the Zeeman interaction Hamiltonian, where $\mu_E$ and $\mu_B$ are the electric- and magnetic dipole moment operators, respectively, and $\vec{E}$ and $\vec{B}$ are the (time-dependent) electric- and magnetic-field vectors.

The spectroscopic parameters of the $a^3\Pi_1$, $\nu = 0$ state of CO that are used in the field-free Hamiltonian are given elsewhere [8–15]. The $\Lambda$-doublet splitting between the positive-parity component (upper) and the negative-parity component (lower) of the $J = 1$ level is about 400 MHz while the hyperfine splitting of each parity level of $^{13}\text{CO}$ into $F = 1/2$ (lower) and $F = 3/2$ (upper) sublevels is about one order of magnitude smaller. The body-fixed electric dipole moment $\mu_E = [\mu_E] \in \text{electronically excited metastable state is } 1.3745 \text{ D for both } ^{12}\text{CO} \text{ and } ^{13}\text{CO}[9,10]$. The magnetic moment of the molecule can be expressed as $\hat{\mu} = -\mu_B (g_L \cdot \hat{L} + g_S \cdot \hat{S})$, where $\mu_B$ is the Bohr magneton, $\hat{L}$ is the electron orbital angular momentum operator, $\hat{S}$ is the electron spin operator, and where the magnetic $g$ factors are fixed at the values of the bare electron, $g_L = 1.0$ and $g_S = 2.0023$.

A detailed description of the formalism used to calculate the eigenenergies of the various components of the $J = 1$ level in the $a^3\Pi_1$, $\nu = 0$ state of both $^{12}\text{CO}$ and $^{13}\text{CO}$ in combined electric and magnetic fields is presented in the Appendix. The formalism has been set up for mutually orthogonal static electric and magnetic fields. As is discussed below, this is also adequate to treat the actual situation, in which the electric field rotates with a constant frequency in a plane perpendicular to the magnetic field. In Fig. 4 we only show the outcome of these calculations in the form of plots of the energy levels for the upper $\Lambda$-doublet component of $^{12}\text{CO}$ and $^{13}\text{CO}$ as a function of electric-field strength in the absence (left column) or in the presence of a 50-G magnetic field (right column). At low electric-field strengths, the Stark shift is quadratic, but as the electric-field strength increases and $|H_Z|$ becomes much larger than $|H_{\text{A,bfs}}|$ and $|H_{\text{S}}|$, the Stark energy shows a linear dependence on the electric-field strength; that is, $\Delta E_S \propto -\Omega M^J_E \mu_E E$, and the product of the projection of the electronic angular momentum along the internuclear axis $\Omega$ and the projection $M^J_E$ of the angular momentum $\hat{J}$ on the electric-field vector $\vec{E}$ becomes an approximately good quantum number. If a weak magnetic field such as that present in the experiment is applied in the absence of an electric field, each of the zero-field levels splits into $(2J + 1)$ [or in $(2F + 1)$] separate levels based on their $M^J_E$ (or $M^F_E$) quantum number. The Zeeman energy is linear in magnetic field and can be calculated using first-order perturbation theory as $\Delta E_Z \approx \mu_{\text{eff}} M B$, where $M = M^J_E$ (or $M^F_E$) and $\mu_{\text{eff}} \sim \mu_B$ describes the effective magnetic moment of a particularparity and, in the case of $^{13}\text{CO}$, particular $F$ component. When a strong electric field is applied to the molecule in addition to the magnetic field, such that $|H_S| \gg |H_{\text{A,bfs}}|,|H_Z|$, the energy levels can again be characterized with the approximately good quantum number $\Omega M^J_E$ and show a linear Stark shift.

The behavior of the eigenenergies in static electric and magnetic fields is quite instructive in describing the
nonadiabatic transitions—and thus losses—of molecules from the low-field-seeking states \((\Omega M_J^F = -1)\) to nontrappable \((M_J^F = 0)\) states. Near the edge of the trap, where the electric field is as high as 4.2 kV/cm, the Stark effect provides an energy gap of about \(U_{\text{gap}} = 60\) mK \(\approx 1.3\) GHz between low-field-seeking states and nontrappable states. Since this is much larger than both the frequency of the motion of the molecules in the traps and the frequency of the applied waveforms, nonadiabatic losses will not occur near the edge of the trap. In the vicinity of the trap center, however, this argument no longer holds, and the eigenfunctions can change from \(M_J^F\)-type wave functions to \(M_J^F\) type (or \(M_J^F\) type) at a rate faster than the energy gap \(E_{\text{gap}}\) in that region. In the case of a \(^{12}\)CO molecule, the energy gap at the center of the trap goes to zero in the absence of a magnetic field. If a molecule in a low-field-seeking state flies near the trap center with a velocity \(v\) high enough, or with a distance of closest approach \(b\) small enough, that the corresponding interaction time with the trap center \(\tau = b/v\) no longer fulfills the adiabaticity condition, that is, when the condition \(E_{\text{gap}} \gg h/\tau\) no longer holds, then the probability of transitions to nontrappable states can become significant. In the absence of a magnetic field, \(^{13}\)CO molecules are much safer from such nonadiabatic losses due to the energy gap of 50 MHz between the \(F = 3/2\) level (which becomes low-field-seeking in an electric field) and the \(F = 1/2\) level (which correlates with nontrappable \(M_J^F = 0\) states).

**B. Calculating rates for nonadiabatic transitions**

The basic idea underlying the calculation of the nonadiabatic losses for the molecules in low-field-seeking states is that, since the transitions to nontrappable states happen primarily as the molecules pass the zero-field region at the center of a microtrap, the overall loss probability can be estimated by first calculating the loss probability in a single pass. For simplicity, the trajectory of the CO molecule is assumed to have a constant velocity; this is reasonable, since the forces on the molecule moving in the trap, is a function of both position \(r(t)\) (due to the inhomogeneous field distribution) and time \(t\) (due to the rotation of the field vectors relative to the trap center), as discussed in Sec. II. The time-dependent Hamiltonian that the molecule experiences is calculated by assuming a position in time given by \(r(t) = (vt - x_{\text{init}})\hat{\mathbf{x}} + b\hat{\mathbf{y}}\), which corresponds to the molecule moving with a constant velocity \(v\) and approaching the trap center with a minimum distance \(b\). The variable \(x_{\text{init}}\) must be chosen such that the initial position \(r(0) = -x_{\text{init}}\hat{\mathbf{x}} + b\hat{\mathbf{y}}\) is sufficiently far from the center such that at \(r(0)\) the adiabaticity condition is still satisfied.

The initial state of the molecule could be chosen as a low-field-seeking eigenstate of the instantaneous Hamiltonian at the initial position and time. If the electric-field vector is rotating, however, the wave function of the molecule will immediately accumulate amplitude in other quantum states, even if the magnitude of the electric field is constant. The amplitude that appears in other states will only be negligible if the energy splitting between them and the initial state is much larger than the rotation frequency. Alternatively, one can choose an initial state that is a stationary state in the rotating system, as is discussed below. The calculation of the transition probability as the molecule flies past the field minimum can then be started at lower fields, that is, with a smaller value of \(x_{\text{init}}\).

In the current system, the magnetic-field vector is oriented along the \(\hat{\mathbf{z}}\) axis and the electric-field vector lies in the \(xy\) plane. If the angle of the electric-field vector with respect to the \(+\hat{\mathbf{x}}\) axis (toward the \(+\hat{\mathbf{y}}\) axis) is given by \(\phi\), the Hamiltonian of the molecule can be computed by rotating the physical system around the \(\hat{\mathbf{z}}\) axis through an angle \(-\phi\), operating on it with a Hamiltonian \(\hat{H}'\) which corresponds to a system with the same magnetic-field vector and in which the electric field has the same magnitude but is directed along the \(+\hat{\mathbf{x}}\) axis, and then rotating the physical system back through an angle \(\phi\). In operator form, this can be written as

\[
\hat{H} = e^{-i\hat{F}_z\phi} \hat{H}' e^{i\hat{F}_z\phi},
\]

where \(\hat{F}_z\) is the total angular momentum of the molecule along the \(\hat{\mathbf{z}}\) axis. Using this form of \(\hat{H}\), Eq. (4) can be rewritten as

\[
\hat{h} \frac{\partial \psi_Q}{\partial t} = \left(\hat{H}' - \hat{F}_z \hat{\partial}_z \phi'\right) \psi_Q.
\]

where \(\psi_Q = e^{i\hat{F}_z\phi} \psi\). This equation has the same form as Eq. (4) and can be solved in the same way as the time-independent Schrödinger equation if the magnetic field is constant, the electric-field strength is constant, and the electric-field vector rotates at a constant frequency. The eigenvalues that result are called “quasienergies” and \(\hat{H}_Q = \hat{H}' - \hat{F}_z \hat{\partial}_z \phi'\) is the quasienergy Hamiltonian \([16,17]\). A similar approach has been used in the recent work by Wall et al. \([3]\).

In Sec. II it was shown that the angle of the electric field in the \(xy\) plane \(\phi' = \phi_0 - \phi + \pi\) contains contributions from both the angular coordinate of the molecule with respect to the trap center \(\phi\) and a phase that results from the constant rotation of the field vectors as the traps move over the chip \(\phi_0 = 2\pi \frac{B}{c} t\). Because \(\phi_0\) increases linearly in time, the contribution of \(\phi_0\) to the quasienergy Hamiltonian is time independent, having
the form \(-\hbar v_0 \hat{F}_z\). This operator is diagonal in the basis sets used for both \(^{12}\)CO and \(^{13}\)CO, and in the case of \(^{12}\)CO it is exactly equivalent to the Zeeman interaction for each energy eigenstate. As the rotation frequency \(v_0\) is 3.75 MHz when the molecules are guided with 300 m/s over the chip, its contribution to the quasienergy Hamiltonian is equivalent to a magnetic field of about \(-8\) G. It should be understood, however, that we are not dealing with a real magnetic field produced by the rotating electric field here; the effect of a rotating coordinate system merely produces a shift to the quasienergies that resembles the Zeeman Hamiltonian but does not depend on the magnetic moment. In the case of \(^{13}\)CO, the rotation frequency is not equivalent to a Zeeman interaction since, as stated in the definition of \(\hat{\mu}\), the gyromagnetic factors of the orbital angular momentum and the electron spin are different.

For the subsequent calculations, the quasienergy eigenvector instead of the normal Hamiltonian eigenvector is chosen as the initial state. After choosing an initial state \(i\) at the position \(r(0) = -x_{\text{min}} \hat{x} + b \hat{y}\), the quasienergy vector is propagated in time using Eq. (6) until the molecule reaches the position \(r(\text{final}) = x_{\text{min}} \hat{x} + b \hat{y}\). The final state is then expressed in terms of quasienergy eigenvectors at the final position and time, and the probability of the molecule ending up in a state \(j\), \(P_{i,j}(v,B,b)\), is calculated. For all calculations, the population is assumed to be initially distributed equally over all low-field-seeking levels, two for \(^{12}\)CO and four for \(^{13}\)CO. The calculation of \(P_{i,j}(v,B,b)\) only needs to be carried out for the initial state \(i\) corresponding to the \(M_F^j = +1\) low-field-seeking level, since the \(M_F^j = 0\) low-field-seeking level is completely stable against nonadiabatic transitions (see the Appendix). For \(^{13}\)CO, none of the four low-field-seeking levels is stable against nonadiabatic transitions at all magnetic fields, so \(P_{i,j}(v,B,b)\) must be calculated for each initial level \(i\).

In the end, we are interested in the probability \(T(B)\) of a molecule remaining in a low-field-seeking state for the duration of its time in the microtrap, as this is the quantity that is measured in the experiment. For \(^{12}\)CO molecules in the ideal case, that is, when the electric field is perfectly perpendicular to the magnetic field and the traps move perfectly smoothly over the chip, the survival probability for a single molecule in a single state is given by the product of its survival probabilities after each individual encounter with the trap center. The overall transmission probability \(T(B)\) is then calculated by averaging this over both low-field-seeking states and over \(N\) molecules:

\[
T(B) = \frac{1}{N} \sum_{n=1}^{N} \left[ \frac{1}{2} \prod_{k=1}^{K} P_{M_F^0=0,M_F^0=0}(v_{n,k},B,b_{n,k}) + \frac{1}{2} \prod_{k=1}^{K} P_{M_F^j=1,M_F^j=1}(v_{n,k},B,b_{n,k}) \right] .
\]

The total number of passes \(K\) of each molecule and the speed \(v_{n,k}\) and closest approach distance \(b_{n,k}\) of the \(k\)th pass of the \(n\)th molecule are determined using simulations of the classical trajectory of a molecule in the trap, as described elsewhere [7]. Since the \(M_F^j = 0\) state is completely stable, \(P_{M_F^j=0,M_F^j=0}(v_{n,k},B,b_{n,k}) = 1\), and the transmission probability \(T(B)\) in the ideal case can never be less than \(1/2\). For \(^{13}\)CO, calculating \(T(B)\) is somewhat more complicated, since the \(F = 3/2, M_F^j = +3/2\) low-field-seeking level and the \(F = 3/2, M_F^j = -1/2\) low-field-seeking level are coupled, as are the \(F = 3/2, M_F^j = +1/2\) and \(F = 3/2, M_F^j = -3/2\) levels. During each encounter with the trap center, a molecule in a particular low-field-seeking state can transition not only to a nontrappable state but also to one other low-field-seeking state. To calculate the transmission probability of a single \(^{13}\)CO molecule, the population in each low-field-seeking state after an encounter with the trap center is computed based on the population distribution before the encounter, and the total population still in a low-field-seeking state after the last pass is recorded. As in \(^{12}\)CO, \(T(B)\) is obtained by averaging the result of this calculation over a large number of molecules.

To accurately describe the experimental data, the theoretical calculations must be extended to include the jittering motion of the traps and the nonperpendicularity of the electric and magnetic fields. The jittering motion is accounted for by including the full motion of the center of the trap as shown in Fig. 3 in the calculation of the transition probability \(P_{i,j}(v,B,b,\phi)\). As in the ideal case, the transition probability depends on speed \(v\), magnetic field \(B\), and closest approach distance \(b\) (although this distance is now defined relative to the average position of the minimum instead of the actual position). Additionally, the transition probability now also depends on the time \(t\) at which the molecule arrives relative to the jittering cycle and the direction \(\phi\) from which it comes. If the electric and magnetic fields are not exactly perpendicular, low-field-seeking states that are normally decoupled can mix. In \(^{12}\)CO, the \(M_F^j = 0\) and \(M_F^j = +1\) states, which converge asymptotically at high electric fields, then become coupled. As a result, the population can partially redistribute between these two levels while the molecule is in a region of high electric field between successive encounters with the trap center. To account for this effect, it is assumed in the calculations that, after each encounter with the trap center, a molecule’s population \(n\) in each of these two low-field-seeking states is redistributed such that

\[
n_{M_F^j=+1}' = (1 - m)n_{M_F^j=+1} + mn_{M_F^j=0} , \quad (8)\\
n_{M_F^j=0}' = (1 - m)n_{M_F^j=0} + mn_{M_F^j=+1} , \quad (9)
\]

where \(n'\) is the new population distribution. The parameter \(m\) describes the degree of the redistribution; at the extremes, a value of 0 indicates that no redistribution occurs while a value of 1/2 corresponds to complete redistribution. Its exact value is difficult to predict and should actually depend on the trajectory of the molecule. For simplicity, \(m\) is determined by fitting it to the data; note that this is the only fitting parameter used. For \(^{13}\)CO, remixing can occur at high electric fields between the \(F = 3/2, M_F^j = -3/2\) and the \(F = 3/2, M_F^j = -1/2\) levels and also between the \(F = 3/2, M_F^j = +1/2\) and the \(F = 3/2, M_F^j = +3/2\) levels. The remixing coefficient \(m\) can be different for each of these pairs of levels, and thus for \(^{13}\)CO, two fitting parameters are necessary.
IV. EXPERIMENTAL RESULTS

To measure the effectiveness of the magnetic field at suppressing nonadiabatic losses, metastable CO molecules are guided over the full length of the chip at a constant velocity of 300 m/s and are subsequently detected using laser ionization. Measurements are carried out for both positive and negative magnetic fields, where the direction of positive magnetic field coincides with the +z axis (see Fig. 1). To compensate for longterm drifts in the intensity of the molecular beam, the parent ion signal is measured with the magnetic field on and with the magnetic field off, and the ratio between these two measurements is recorded. In Fig. 5, the thus-recorded relative number of $^{12}$CO (top panel) and $^{13}$CO (bottom panel) molecules that are guided over the chip is shown as a function of the applied magnetic field. Both the measurements with the standard waveforms and with the improved waveforms are shown in the top panel.

It is clear from the data shown in Fig. 5 that, as the magnetic-field strength increases, the number of $^{12}$CO molecules reaching the detector increases. This is as expected because the splitting between the low-field-seeking levels of $^{12}$CO and the nontrappable level increases with the magnetic-field strength, thereby increasingly suppressing nonadiabatic losses. The measurements with the improved waveforms show that at magnetic fields more negative than $-40$ G and more positive than $+50$ G, the number of guided molecules becomes constant, indicating that all nonadiabatic losses are suppressed under these conditions. The data have been scaled vertically such that the saturation observed at high magnetic-field strengths corresponds to a transmission of unity. The ratio between the signal at high magnetic field and low magnetic field is smaller than when the standard waveforms are used, implying that the improved waveforms also reduce the losses without a magnetic field. The number of $^{13}$CO molecules reaching the ionization detector, on the other hand, is seen to decrease as a function of magnetic field. The vertical scale in this case is based on the results of the theoretical calculations at low magnetic-field strengths (vide infra). The bottom panels of Fig. 4 show that the $M_B = \pm 1/2$ level of the nontrappable $F = 1/2$ state increases in energy in a magnetic field, while the $M_B = -3/2$ and $M_B = -1/2$ levels of the low-field-seeking $F = 3/2$ state are at the same time lowered in energy. This reduction of the energy gap between the low-field-seeking and nontrappable levels enhances the nonadiabatic losses. Both the $^{12}$CO and the $^{13}$CO data are slightly asymmetric for positive and negative magnetic fields. The data for $^{12}$CO indeed seem to be symmetric around a magnetic field of about $+8$ G, as expected from the theoretical model.

The results of the theoretical models are shown as solid curves in Fig. 5 as well. The thick solid curves in the top and the bottom panels result from the theoretical model for the ideal case, that is, when the jittering of the traps would be absent and no remixing would occur between decoupled states. The width of the theoretically predicted transmission minimum for $^{12}$CO around $+8$ G depends sensitively on the relative velocity between the CO molecule and the center of the trap as they pass and gets larger with increasing velocities. In the case of $^{13}$CO, two narrow transmission minima are expected around $-65$ and $+90$ G, corresponding to fields at which the the $F = 1/2$, $M_B = +1/2$ and $F = 3/2$, $M_B = -3/2$ levels cross, and between these two minima, no losses are expected. As in $^{12}$CO, the width of the transmission minima increases as the relative velocity between the molecules and the trap center increases. It is clear from the comparison of these theoretical curves with the experimental data that the observed measurements cannot be quantitatively explained if the traps are assumed to move smoothly over the chip; the jittering of the traps must be taken into account.

The transmission probabilities calculated for the case in which the jittering is explicitly taken into account are seen to almost quantitatively agree with the measurements. In particular, the theoretical curves reproduce the asymmetry between the intensity of the guided $^{12}$CO molecules at positive and negative magnetic fields as well as the narrowing of the profiles when the waveforms are improved. In the calculations for $^{12}$CO, a partial redistribution after each pass of 18% ($m = 0.09$) has been assumed for the standard waveforms and 12% ($m = 0.06$) for the improved waveforms. It cannot be excluded that the jittering of the traps was still slightly more severe during the actual experiments than shown for the standard waveforms in Fig. 3, which would explain.

FIG. 5. (Color online) Measured signal of $^{12}$CO (top panel) and $^{13}$CO (bottom panel) molecules guided over the chip at 300 m/s as a function of the magnetic field. The vertical scaling of the individual data sets is described in the text. Measurements have been performed using the standard waveforms (solid circles) for both $^{12}$CO and $^{13}$CO; for $^{12}$CO, measurements with the improved waveforms (open circles) are shown as well. The simulated curves of the transmission probability $T(B)$ are shown as solid curves that overlay the data points. The thick solid curves in the top and bottom panels result from the theoretical model for the ideal case. The red dashed curves show the prediction of the theoretical model for the survival probability of molecules decelerated from 300 m/s to zero velocity in 250 $\mu$s.
the experimentally observed additional broadening for that case. In the $^{13}$CO calculations, the best agreement with the experimental data was found when assuming no remixing between the $M_F = +3/2$ and the $M_F = +1/2$ levels and 30% remixing ($m = 0.15$) between the $M_F = -1/2$ and the $M_F = -3/2$ level. The maximum transmission at about +10 G is not sensitive to the remixing coefficients, since the transition probability for each of the low-field-seeking states is about the same in this region. It can be reliably inferred from the theoretical calculations that, even at low magnetic fields, about 1/3 of the $^{13}$CO molecules are lost to nonadiabatic transitions while being guided over the chip. Based on this, the $^{13}$CO data shown in the bottom panel of Fig. 5 have been scaled vertically such that the transmission at zero magnetic field is 2/3.

The theoretical model used to explain the guiding data can also be applied to predict the nonadiabatic losses that are expected to occur during linear deceleration. The red dashed curves in the top (bottom) panel of Fig. 5 show the survival probability of $^{12}$CO ($^{13}$CO) molecules decelerated from 300 m/s to zero velocity in 250 µs. In these calculations, it is assumed that the jittering motion at 300 m/s is that of the standard waveforms. The velocity of the jittering motion is assumed to be proportional to the frequency of the applied waveforms while the latter is reduced from 2.5 MHz to zero. For $^{12}$CO at low magnetic fields, the survival probability during deceleration is only 1/4 of the survival probability of $^{12}$CO guided at a constant velocity of 300 m/s. The magnetic field needed to suppress losses is smaller, however. While the survival probability for guiding is symmetric around a magnetic field of +8 G, the symmetry point for deceleration is shifted closer to zero field, to +4 G, due to the lower rotation frequency of the electric-field vectors in the trap at lower velocities. For $^{13}$CO, the model predicts that the transmission probability during deceleration is larger than for guiding at all magnetic-field strengths.

The differences in transmission probability between guiding and deceleration can result from various effects that either enhance or suppress losses as the deceleration of the trap increases. The smaller spatial acceptance of a strongly accelerated trap results in a larger fraction of the trapped cloud being in the jittering region at any given time, which enhances the losses during deceleration [7]. Losses are also enhanced due to the molecules spending a longer time on the chip. On the other hand, since the average velocity of a decelerating trap is lower than that of a trap at constant velocity, the velocity of the jittering motion is reduced, suppressing nonadiabatic losses. While it is difficult to predict through simple arguments the relative importance of these effects, the outcome of the calculations is corroborated by previous measurements at zero magnetic field, in which it was shown that $^{13}$CO molecules can be decelerated to a standstill while $^{12}$CO molecules are rapidly lost with increasing deceleration [1].

V. CONCLUSIONS

In this paper we have studied the losses due to nonadiabatic transitions in metastable CO molecules—laser-prepared in the upper $\Lambda$-doublet component of the $J = 1$ level in the $a^3\Pi_1$, $v = 0$ state—guided at a constant velocity in microtraps over a chip. Transitions between levels in which the molecules are trapped and levels in which the molecules are not trapped can be suppressed (enhanced) when the energetic splitting between these levels is increased (decreased) by the application of a static magnetic field. For a quantitative understanding of this effect, the energy level structure of $^{12}$CO and $^{13}$CO molecules in combined magnetic and electric fields has been analyzed in detail. When the CO molecules are guided over the chip, they are in an electric field that rotates with a constant frequency; the direction of the externally applied magnetic field is perpendicular to the plane of the electric field. The probability with which either $^{12}$CO or $^{13}$CO molecules are transmitted over the chip, that is, the probability that the molecules stay in a trapped level for the complete duration of the flight over the chip, has been measured as a function of the magnetic field. The observed transmission probability can be quantitatively explained.

To reduce trap losses in future experiments, it will be important to improve the applied waveforms. This will not only reduce losses due to nonadiabatic transitions caused by the jittering, but it will also reduce losses due to mechanical heating. Mechanical losses might also have been present in the current experiment, but because the measurements always compared the guiding efficiency with magnetic field on and off, we have not been sensitive to these losses. Alternatively, it might be possible to avoid the need for improved waveforms by moving the minimum on an orbit that is much larger than the amplitude of the jittering motion, creating a large region around the effective trap center through which the minimum never passes. Such a trap, known as a time orbiting potential (TOP) trap, prevents nonadiabatic losses but is much shallower than a static trap [4].

The intrinsic difficulties with making the waveforms required for the experiments discussed here should be stressed; with present-day technology these waveforms can hardly be made better than we have them now, in particular because, in order to bring molecules to a standstill, we want to be able to rapidly chirp the frequency down from 2.5 MHz to zero. While the $LC$ filter used to produce the improved waveforms reduces the total harmonic distortion of the amplitudes from 7% to 3%, it also makes producing a constant amplitude frequency chirp more complicated. We are nevertheless optimistic that the jittering can be reduced by another factor of two to three relative to the best waveforms that we have used so far. In the case of $^{12}$CO, for instance, a magnetic field of 10 G, applied in the right direction, would then already completely avoid losses due to nonadiabatic transitions. With the present waveforms, trap losses can only be avoided when the applied magnetic fields are made sufficiently high. One should realize that there is an upper limit to these fields, however, as at some point transitions to the lower $\Lambda$-doublet components can be induced, opening up a new loss channel.

The extreme sensitivity to the details of the applied voltages results from the fact that the electric-field minima above the chip originate from the vectorial cancellation of rather large electric-field terms. Design studies are in progress to find an electrode geometry that is less sensitive to imperfections in the applied waveforms. A modified electrode geometry is also required to avoid trap losses at the ends of the tubular
traps. Although the ends are closed in the present geometry by the fringe fields of adjacent electrodes, the electric field near the ends has components along the long axis of the trap, presumably leading to nonadiabatic losses even in the presence of the offset magnetic field.

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APPENDIX: THE a3Π1, v = 0, J = 1 HAMILTONIAN

In this Appendix, the formalism that has been used to calculate the energies of the M components of the J = 1 level in the a3Π1, v = 0 state of both 12CO and 13CO in combined, but mutually orthogonal, static electric and magnetic fields is presented. In the coordinate system used here, the magnetic-field vector is oriented along the z axis and the electric-field vector is in the xy plane. It is thus possible to separate the basis states into two uncoupled sets, consisting of wave functions that are either symmetric or antisymmetric under reflection in the xy plane, thereby reducing the computational complexity. The magnetic field can only couple states of the same parity and magnetic-field vector is in the plane perpendicular to the quantization axis it can only couple states of opposite parity with magnetic field can only couple states of same parity and magnetic-field vector is in the plane perpendicular to the quantization axis it can only couple states of opposite parity with magnetic field.

The + and − sign at the end describe the parity of the basis state. All states with the upper (lower) sign belong to one set. For 12CO there are two sets containing six basis states each:

(i) \( M_B^6 = -1, \pm \); 
(ii) \( M_B^6 = 0, \mp \); 
(iii) \( M_B^6 = 1; \pm \).

The + and − sign at the end describe the parity of the basis state. All states with the upper (lower) sign belong to one set. For 13CO there are two sets containing six basis states each:

(i) \( F = 3/2, M_B^F = -3/2, \pm \); 
(ii) \( F = 1/2, M_B^F = -1/2, \mp \); 
(iii) \( F = 3/2, M_B^F = -1/2, \mp \); 
(iv) \( F = 1/2, M_B^F = 1/2, \pm \); 
(v) \( F = 3/2, M_B^F = 1/2, \pm \); 
(vi) \( F = 3/2, M_B^F = 3/2, \mp \).

Again, all states with the upper (lower) parity belong to one set.

Based on this formalism and using the zero-field spectroscopic parameters and matrix elements given in Refs. [8–15], the corresponding Hamiltonian matrices can be calculated. Without loss of generality, the electric-field vector is taken to be oriented along the z axis, that is, \( \vec{E} = E \hat{z} \). The Hamiltonian matrices for other orientations of the electric-field vector in the xy plane can be computed using the unitary transformation given in Eq. (5); the matrices given here correspond to \( \hat{H}' \) in this equation. The origin of the energy scale for each isotopologue is defined to be the lowest-energy field-free state in the upper Λ-doublet component, as shown in Fig. 4.

For 12CO, the matrices \( \hat{H}_\text{upper} \) and \( \hat{H}_\text{lower} \) for the set of basis states with the upper and lower parity, respectively, are given by

\[
\hat{H}_\text{upper} = \begin{pmatrix}
-R_1 & S & 0 \\
S & -\Lambda & S \\
0 & S & R_1
\end{pmatrix}
\] (A1)

and

\[
\hat{H}_\text{lower} = \begin{pmatrix}
-\Lambda - R_2 & S & 0 \\
S & 0 & S \\
0 & S & -\Lambda + R_2
\end{pmatrix},
\] (A2)

where \( \Lambda = 394.066 \text{ MHz} \),

\( R_1 = (1, + |\hat{H}_Z|1, +) = 0.3332 \mu_B B, \)

\( R_2 = (1, - |\hat{H}_Z|1, -) = 0.3406 \mu_B B, \)

\( \Lambda = (0, + |\hat{H}_Z|1, -) = 0.3513 \mu_B E, \)

and the bra and ket vectors have the form |\( M_F \rangle, \text{parity} \rangle. \)

It is clear from these matrices that the energy level labeled as \( M_B^6 = 0 \) in the case of 12CO (upper right panel of Fig. 4) is only directly coupled to the \( M_B^6 = \pm 1 \) levels of the lower Λ-doublet component and that there is no direct coupling to the nearby \( M_B^6 = \pm 1 \) levels of the upper Λ-doublet component. Provided that the electric and magnetic fields are exactly in combined, but mutually orthogonal, static electric and magnetic fields.

For 13CO, the corresponding matrices for the sets of basis states with the upper and lower parity are given by

\[ \hat{H}_{\text{upper}} = \begin{pmatrix}
E_1 - 3R_3 & \sqrt{3}S_3 & \sqrt{3}S_4 & 0 & 0 & 0 \\
\sqrt{3}S_3 & -E_3 - R_2 & R_4 & S_4 & -S_3 & 0 \\
\sqrt{3}S_4 & R_4 & -E_2 - R_6 & S_2 & S_4 & 0 \\
0 & S_1 & S_2 & R_1 & R_3 & -\sqrt{3}S_2 \\
0 & -S_3 & S_4 & R_3 & E_1 + R_3 & \sqrt{3}S_4 \\
0 & 0 & 0 & -\sqrt{3}S_2 & \sqrt{3}S_4 & -E_2 + 3R_6
\end{pmatrix} \] (A3)

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and

\[ \hat{H}_{\text{lower}} = \begin{pmatrix}
-E_2 - 3R_6 & \sqrt{3}S_2 & \frac{3}{2}S_4 & 0 & 0 & 0 \\
\sqrt{3}S_2 & -R_1 & R_3 & S_1 & -S_2 & 0 \\
\frac{3}{2}S_4 & R_3 & E_1 - R_5 & S_3 & S_4 & 0 \\
0 & S_1 & S_3 & -E_3 + R_2 & R_4 & -\sqrt{3}S_3 \\
0 & -S_2 & S_4 & R_4 & -E_2 + R_6 & \frac{3}{2}S_4 \\
0 & 0 & 0 & -\sqrt{3}S_3 & \frac{3}{2}S_4 & E_1 + 3R_5
\end{pmatrix}, \tag{A4} \]

where \( E_1 = 58.412 \text{ MHz}, \)
\( E_2 = 309.340 \text{ MHz}, \)
\( E_3 = 346.346 \text{ MHz}, \)
\( R_1 = \langle 1/2,1/2, + | \hat{H}_Z | 1/2,1/2, + \rangle = 0.2264 \mu_B B, \)
\( R_2 = \langle 1/2,1/2, - | \hat{H}_Z | 1/2,1/2, - \rangle = 0.2309 \mu_B B, \)
\( R_3 = \langle 1/2,1/2, + | \hat{H}_Z | 3/2,1/2, + \rangle = 0.1600 \mu_B B, \)
\( R_4 = \langle 1/2,1/2, - | \hat{H}_Z | 3/2,1/2, - \rangle = 0.1635 \mu_B B, \)
\( R_5 = \langle 3/2,1/2, + | \hat{H}_Z | 3/2,1/2, + \rangle = 0.1132 \mu_B B, \)
\( R_6 = \langle 3/2,1/2, - | \hat{H}_Z | 3/2,1/2, - \rangle = 0.1155 \mu_B B, \)
\( S_1 = \langle 1/2, -1/2, + | \hat{H}_Z | 1/2,1/2, - \rangle = 0.3313 \mu_B E, \)
\( S_2 = \langle 3/2, -1/2, - | \hat{H}_Z | 1/2,1/2, + \rangle = 0.1172 \mu_B E, \)
\( S_3 = \langle 3/2, -1/2, + | \hat{H}_Z | 1/2,1/2, - \rangle = 0.1172 \mu_B E, \)
\( S_4 = \langle 3/2, -1/2, + | \hat{H}_Z | 3/2,1/2, - \rangle = 0.3313 \mu_B E, \)
and the basis vectors have the form \( |F,M_F,\text{parity} \rangle. \)

If the magnetic field is not perpendicular to the electric field, additional nonzero matrix elements will appear in the Hamiltonian that couple the states of \( \hat{H}_{\text{upper}} \) and \( \hat{H}_{\text{lower}}. \)