Equation of State for Phospholipid Self-Assembly

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ABSTRACT Phospholipid self-assembly is the basis of biomembrane stability. The entropy of transfer from water to self-assembled micelles of lysophosphatidylcholines and diacyl phosphatidylcholines with different chain lengths converges to a common value at a temperature of 44°C. The corresponding enthalpies of transfer converge at ~18°C. An equation of state for the free energy of self-assembly formulated from this thermodynamic data depends on the heat capacity of transfer as the sole parameter needed to specify a particular lipid. For lipids lacking calorimetric data, measurement of the critical micelle concentration at a single temperature suffices to define an effective heat capacity according to the model. Agreement with the experimental temperature dependence of the critical micelle concentration is then good. The predictive powers should extend also to amphiphile partitioning and the kinetics of lipid-monomer transfer.

INTRODUCTION

Spontaneous self-assembly of phospholipids in water is essential to the stability of biological membranes, and indeed to life itself. It is driven by thermodynamics, specifically the tendency of hydrophobic lipid chains to segregate from contact with water, coupled with the structural requirement to form a thin, flexible membrane that functionally forms a tight permeability barrier to polar solutes in the aqueous environment. The latter aspects require a strong interplay of the lipid polar headgroups and their hydrocarbon acyl chains. This results in formation of bilayer membranes or, in the case of shorter or single lipid chains, topologically equivalent normal micelles. Because the lipid chains are highly flexible, the membrane interior provides a fluid microphase of uniquely graded properties. Thus, thermodynamics of lipid assembly are important when considering incorporation and stability of membrane proteins, and also such aspects as partitioning and transmembrane transport of hydrophobic drugs and the interaction with other amphiphiles, in both pharmacological and biotechnological applications.

Until recently, considerably more attention has been paid to thermodynamic analysis of protein folding than to that of lipid-membrane assembly. For a restricted set of globular proteins, it was found that thermal unfolding is characterized by denaturation entropies and enthalpies per residue that extrapolate to common values at temperatures in the region of 110°C (1). Also, the entropy for transfer of hydrocarbons to water goes to zero at a temperature close to this range (2). These features led to a thermodynamic description of protein unfolding in terms of the linear dependence of denaturation entropy and enthalpy on heat capacity of unfolding (3). Although entropy and enthalpy convergence is not preserved with an expanded set of thermodynamic data on protein unfolding (4), it still holds for the simpler process of transferring small apolar molecules from hydrophobic environments to water (see, e.g., (5)).

Here, I explore to what extent these common features of the hydrophobic effect, namely entropy and enthalpy convergence coupled with a large heat capacity for transfer from water to apolar environments, can be used to describe the self-assembly of phospholipids into micelles or membranes. Lipid assembly relates more directly to small-molecule transfer processes than does the structurally more complex situation accompanying protein unfolding. My aim is to establish an equation of state for self-assembly of lipid monomers in water that applies with reasonable generality to all phospholipids. In addition to the fixed parameters that we need to define this equation of state, the thermodynamics for a particular lipid are determined by a single further parameter, the heat capacity of transfer to the micelle, or alternatively, the value of the critical micelle concentration (CMC) at a single temperature. It is to be expected, and is found, that the thermodynamic parameters for lipid self-assembly differ significantly from those for the hydrophobic effect alone, because of contributions from the structurally necessary phospholipid polar headgroups.

Similar thermodynamic principles should apply to the partitioning of aqueous amphiphiles into membranes, which is directly analogous to incorporation into the membrane of constituent lipid monomers. They are relevant also to the kinetics of transfer of lipid monomers into and out of micelles or membranes, because these depend partly on the thermodynamics of partitioning. Both of these aspects are discussed in the context of the equation of state.
RESULTS

Fig. 1 shows the temperature dependence of the entropy and enthalpy for transfer of saturated acyl lysophosphatidylcholines \( (n:0) \text{LPC} \) and diacyl phosphatidylcholines \( (n:0)_2 \text{PC} \) of different chain lengths, \( n \), from the monomeric state in water to their respective micelles. This data is obtained from isothermal titration calorimetry by Heerklotz and Epand (6). In this type of experiment, a concentrated aqueous suspension of micelles is injected into a fixed volume of water, and the heat evolved or absorbed on dissociation of the micelles into monomers dissolved in water is measured. Both the enthalpy and entropy of transfer are strongly dependent on temperature, implying a large heat capacity. To a reasonable degree of approximation, the transfer entropies reach a common value of 50 \( \text{kJ mol}^{-1} \text{K}^{-1} \) in the region of 50°C, whereas the enthalpies extrapolate to a common value of 15 \( \text{kJ mol}^{-1} \) at a temperature below 0°C. There are slight differences between the convergence for lysolipids and for short-chain diacyl lipids, which might be attributable to some difference in structure of their micelles.

Following the treatment of protein unfolding by Murphy et al. (3), I assume that the enthalpy of transfer, \( \Delta H^\text{tr} \), of a lipid monomer from water into the aqueous micellar assembly converges to a common value \( \Delta H^+ \) at temperature \( T^+ \), where \( \Delta C_p^\text{tr} \) is the (temperature-independent) heat capacity of transfer. In Eq. 1, \( \Delta H^+ \) is independent of the lipid chain length \( n_{CH} \) and therefore \( \partial \Delta H^\text{tr} / \partial n_{CH} = 0 \) at the convergence temperature \( T^+ \). Similarly, I assume that the entropy change \( (d\Delta S^\text{tr} = \Delta C_p^\text{tr} dT/T) \) in this same transfer process converges to a common value \( \Delta S^+ \) at temperature \( T^+ \),

\[
\Delta H^\text{tr}(T) = \Delta H^+ + \Delta C_p^\text{tr}(T - T^+), \tag{1}
\]

\[
\Delta S^\text{tr}(T) = \Delta S^+ + \Delta C_p^\text{tr} \ln(T/T^+), \tag{2}
\]

where \( \Delta S^+ \) is independent of lipid chain length, and therefore \( \partial \Delta S^\text{tr} / \partial n_{CH} = 0 \) at \( T = T^+ \). Note that for limited temperature ranges \( (T - T^+ << T^+) \), expansion of the logarithm in Eq. 2 gives a linear temperature dependence: \( \ln(T/T^+) \approx (T - T^+/T^+) \). According to Eqs. 1 and 2, a direct consequence of convergence is that, at any fixed temperature, both enthalpy and entropy should be linearly dependent on the heat capacity of transfer, with a common gradient and intercept for the family of compounds under question (3).

Fig. 2 plots the values of \( \Delta H^\text{tr} \) and \( \Delta S^\text{tr} \) at 25°C, interpolated from the data of Fig. 1, against the constant heat capacity \( \Delta C_p^\text{tr} \) that is deduced from the temperature dependence in the same figure (see also (7,8)). Both entropy and enthalpy

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**FIGURE 1** Temperature dependence of the entropy \( \Delta S^\text{tr} \) (upper panel) and enthalpy \( \Delta H^\text{tr} \) (lower panel) of lipid monomer transfer from water to micelles of saturated 1-acyl lysophosphatidylcholines \( (n:0) \text{LPC} \) (solid symbols and lines) and 1,2-diacyl phosphatidylcholines \( (n:0)_2 \text{PC} \) (open symbols and dashed lines) of different chain lengths, \( n \). Experimental data from Heerklotz and Epand (6).

**FIGURE 2** Dependence of the transfer entropy \( \Delta S^\text{tr} \) (upper panel) and enthalpy \( \Delta H^\text{tr} \) (lower panel), from water into micelles at 25°C, on heat capacity of transfer \( \Delta C_p^\text{tr} \) for the lysophosphatidylcholines and diacyl phosphatidylcholines of Fig. 1 (solid squares). Solid lines are linear regressions according to Eqs. 1 and 2 (regression coefficients: 0.971 and -0.952, respectively). Open squares are corresponding data for charged lipids \( (8:0)_2 \text{PG} \) and \( (8:0)_2 \text{PA} \) in 0 and 0.15 M NaCl, from Marsh (7).
are approximately linear with respect to the heat capacity for the combined data from lysophosphatidylcholines and diacyl phosphatidylcholines, which are given by the solid symbols in Fig. 2. Linear regression according to Eqs. 1 and 2 gives the following aggregate parameters for these zwitter-ionic phospholipids: \( \Delta H^+ = 20.8 \pm 2.3 \text{ kJ mol}^{-1} \), \( T_H^* = -17.6 \pm 4.7^\circ C \), \( \Delta S^+ = 64.0 \pm 4.3 \text{ J mol}^{-1} \text{ K}^{-1} \), and \( T_S^* = 44.2 \pm 2.8^\circ C \). The open symbols in Fig. 2, which are not part of the linear regression, are corresponding data for the negatively charged diacyl phospholipids phosphatidylglycerol (8:0)2PG and phosphatidylserine (8:0)2PS, in 0 and 0.15 M NaCl (7). These data suggest that the parameters for phosphatidylcholines might also represent other phospholipids reasonably well.

From Eqs. 1 and 2, the free energy for transfer of a phospholipid monomer from water into the micelle becomes

\[
\Delta G_{tr}^v(T) = \Delta H^+ - T \Delta S^+ + \Delta C^v_p(T - T_H^* - T \ln(T/T_S^*)),
\]

which is determined by the value of the heat capacity for the particular lipid, together with the aggregate parameters that are obtained from Fig. 2. Equation 3 therefore constitutes an equation of state for the self-assembly of aqueous phospholipids into micelles or membranes. Fig. 3 shows the temperature dependence of the free energy of transfer that is predicted by Eq. 3 for the different phosphatidylcholines from their heat capacities. The free energy displays a minimum that occurs at the temperature \( T_{\text{min}, \Delta G} = T_S^* \exp(-\Delta S^+ / \Delta C^v_p) \), at which the entropy of transfer, \( \Delta S_p = -\partial \Delta G_{tr}^v / \partial T \), is zero. This is the temperature at which the self-assembled state is most stable, and varies systematically between phospholipids according to their heat capacity of transfer. As can be seen from the data points that are also included in the figure, the predictions of Eq. 3 describe the experimental temperature dependence reasonably well over the range of measurement (6). The agreement is not perfect, as might be anticipated from the scatter about the linear regressions in Fig. 2, but we see that Eq. 3 serves quite well in the spirit of a global approximation.

With fixed parameters \( \Delta S^+ \), \( \Delta H^+ \), \( T_S^* \), and \( T_H^* \), for the two convergence points, Eq. 3 reasonably describes the temperature dependence for the whole range of phosphatidylcholines, without further adjustable parameters. However, offsets in absolute values of the free energy are observed for certain lipids. In particular, the absolute values for (10:0)LPC and (6:0)2PC are rather close, but their predicted relative positions are reversed compared with experiment. This suggests that a slight adjustment in effective heat capacity for particular lipids could remove these minor offsets. For instance, decreasing the absolute value of \( \Delta C^v_p \) for (6:0)2PC by 6%, and increasing that of (10:0)LPC by 2%, reverses the predicted order and brings the free energies close to the experimental values. Indeed, we can extend this method to apply the equation of state with phospholipids for which we lack calorimetric measurements. In principle, the CMC determined at a single temperature (as is often the case) should suffice.

For large micelles, or extended bilayers, the free energy for incorporating monomers from water is related to the CMC by (see, e.g., Cevec and Marsh (9))

\[
\Delta G_{tr}^v = RT \ln X_{\text{CMC}},
\]

where \( X_{\text{CMC}} \) is the critical micelle concentration of the lipid monomer, in mole fraction units with respect to water. Rearranging Eqs. 3 and 4, we can then calculate an effective heat capacity of transfer from the CMC measured at temperature \( T \):

\[
\Delta C_{tr}^v_{\text{eff}} = \frac{RT \ln X_{\text{CMC}} - \Delta H^+ + T \Delta S^+}{T - T_H^* - T \ln(T/T_S^*)}.
\]

Table 1 lists the effective heat capacities for lysophosphatidylcholines and diacyl phosphatidylcholines that we obtain in this way. Where heat capacity measurements are available, these are also listed for comparison (cf. Fig. 2). In most cases, we see that the adjusted values of the heat capacity lie within the uncertainty limits of the experimental measurements. Note that the shorter-chain diacyl phosphatidylcholines that we
phosphatidylcholines in Table 1 form micelles, whereas those with longer chains form bilayers. This point is addressed in the Appendix.

Table 1 gives data analogous to Table 1, but for the charged lipids phosphatidylglycerol, phosphatidylserine, and phosphatidic acid. Using the fixed parameters for the equation of state that are established with phosphatidylcholines, we see that the effective heat capacities calculated for a single CMC sometimes do not agree so well with direct measurements as does the same comparison for phosphatidylcholines in Table 1. However, the number of temperature points for those anionic lipids where the heat capacity has been measured is less than for phosphatidylcholines, and the experimental scatter is greater. Nevertheless, we can test whether the parameters established for phosphatidylcholine are appropriate for a different phospholipid by using a systematic comparison of the temperature dependence for spin-labeled phosphatidylglycerol and the

R.T., room temperature; \( \Delta C_{P,\text{eff}} \), effective heat capacity of transfer.

\(^*\)Direct measurements of the heat capacity for transfer of monomers from water.
corresponding phosphatidylcholine that was obtained with electron paramagnetic resonance spectroscopy (15). Fig. 5 compares the experimental temperature dependence of the CMCs for (12:0/4-DOXYL5:0)PG and (12:0/4-DOXYL5:0)PC with predictions from Eq. 3 that use the effective heat capacities found for these lipids in Tables 2 and 1, respectively. For both phospholipids, the sn-1 chain is lauroyl (C12:0), and the sn-2 chain is valeroyl (C5:0) with the DOXYL (4β,4γ-dimethyloxazolidine-N-oxyl) spin label attached at the 4-C atom. As we see, the temperature dependence is well described for the anionic phosphatidylglycerol with the same fixed parameters in the equation of state as for the zwitterionic phosphatidylcholine. Note that these spin-labeled lipids have a short sn-2 chain and both form micelles in water.

DISCUSSION

The equation of state derived here is for assembly/disassembly of lipid micelles or membranes in water. It refers directly to the thermodynamics that govern the stability of biomembranes. On the other hand, theoretical analyses of the hydrophobic effect often are based on the transfer of an apolar molecule from a fixed position in an ideal gas to a fixed position in bulk water (see, e.g., Graziano and Lee (5)). This differs significantly from the process actually involved in self-assembly of lipids in water. A major part of the entropy change accompanying this gas-to-solution transfer is attributed to cavity formation in water (5,30,31). Quite apart from the specific role played by the lipid polar headgroups, we do not expect the convergence temperatures found here to correspond with those predicted by theoretical models for the hydrophobic effect, because the reference states involved are so different. It is known, for instance, that lipid membrane surfaces have a pronounced influence on the ordering of water molecules, which among other things markedly affects the thermodynamics of lipid chain melting and gives rise to strong repulsive forces between zwitterionic bilayers (see, e.g., Cevc and Marsh (9,32)).

Table 3 gives the thermodynamic parameters for convergence that are derived from plots such as those given in Fig. 2 for different transfer processes, and for the original limited data set on protein thermal unfolding that gave rise to this type of analysis. Whereas the entropy and enthalpy of protein unfolding both converge at ~100°C, this is not the case for the various transfer processes. Also, the convergence temperatures differ between the different transfer processes, particularly for the enthalpy. We see

![Figure 5](image-url)
TABLE 3 Parameters for the Equation of State, Eq. 3, Applied to Different Thermodynamic Processes

<table>
<thead>
<tr>
<th>Process</th>
<th>$T_s^*$ (°C)</th>
<th>$\Delta S^{29}$ (J mol$^{-1}$ K$^{-1}$)</th>
<th>$T_H^*$ (°C)</th>
<th>$\Delta H^{29}$ (kJ mol$^{-1}$)</th>
<th>Reference</th>
</tr>
</thead>
<tbody>
<tr>
<td>PC transfer</td>
<td>44 ± 3</td>
<td>64 ± 4</td>
<td>-18 ± 5</td>
<td>21 ± 2</td>
<td>(6)</td>
</tr>
<tr>
<td>Protein unfold</td>
<td>110 ± 6</td>
<td>18 ± 1</td>
<td>102 ± 5</td>
<td>5.7 ± 0.3</td>
<td>(33)$^b$</td>
</tr>
<tr>
<td>Peptide transfer</td>
<td>104 ± 12</td>
<td>15 ± 3</td>
<td>72 ± 9</td>
<td>11.5 ± 0.8</td>
<td>(34)</td>
</tr>
<tr>
<td>HC transfer</td>
<td>106 ± 5</td>
<td>-6 ± 4</td>
<td>40 ± 6</td>
<td>6 ± 2</td>
<td>(27)$^c$</td>
</tr>
<tr>
<td></td>
<td>124 ± 3</td>
<td>74 ± 3</td>
<td>93 ± 2</td>
<td>1.6 ± 0.7</td>
<td>(35)$^d$</td>
</tr>
</tbody>
</table>

$^a$PC transfer is the transfer of diacyl phosphatidylcholine and lysophosphatidylcholine monomers to micellar aggregates. Protein-unfold is the thermal unfolding of globular proteins per residue. Peptide transfer is the dissolution of solid cyclic dipeptides, GG, AG, AA, LG, and VV, per residue in water. HC transfer is the dissolution of liquid aromatic and aliphatic hydrocarbons in water (27), or of gaseous $n$-alkanes (35).

$^b$For a limited range of proteins (33), and excluding parvalbumin (see Murphy et al. (3)).

$^c$Excluding propylbenzene (see Murphy et al. (3) and Baldwin (2)).

$^d$For $C_nH_{2n+2}$ for $n = 2–8$.

This introduces further chain-length-dependent contributions that result in different dependences on $\Delta C_{p,v}$ (see Eqs. 7–9 given later below). Note the large difference in absolute values of the thermodynamic quantities for the two reference states in Fig. 6. Taking the gaseous phase as reference results in most of the enthalpy and a large part of the entropy coming from transfer from the gas to a condensed phase, a process entirely unrelated to lipid self-assembly in water. Indeed, for the liquid alkanes that are included in both data sets in Fig. 6, the gas-phase values are obtained by adding the large heat or entropy of vaporization (36).

The convergence temperatures found here for phospholipid self-assembly depart most from those of the other systems listed in Table 3 (and from theoretical estimates of the hydrophobic effect (5,30)). This is most likely because the reference state for transfer is very different, namely either membrane or micelle, and not simply a homogeneous condensed phase. As mentioned already, the divergent value of $T_H^*$ for the transfer entropy most likely originates from ordering of water molecules at the membrane/micelle surface.

Having established that phospholipid self-assembly might reasonably be represented by Eq. 3, it now remains to ask why and to what extent. Lee (37) has shown that entropy and enthalpy converge if each is a bilinear function of temperature and some intensive property of the solute (such as chain length, $n_{CH}$). On the other hand, Gill and Wadsö (27) have derived an expression for the free energy of dissolving aliphatic and aromatic hydrocarbons in water that is based on linear dependences on the number of H-atoms in the solute that are directly bonded to carbon. For our case of lipid self-assembly, the free energy for transfer of lipid monomers from water into micelles that we derive from the experimental CMC depends approximately linearly on the number of aliphatic carbon atoms, $n_{CH}$, in the chains ((8) and see Fig. 7 later in the Appendix),

$$\Delta G_p^v(T) = \left( \frac{\partial \Delta G_p^v(T)}{\partial n_{CH}} \right) \times n_{CH} + \Delta \Delta G_p^v(T), \quad (6)$$

where $\Delta \Delta G_p^v(T)$ specifies the end contributions, which are given by the intercept of the linear dependence. This linearity with chain length corresponds to the conventional interpretation of the hydrophobic effect: that the free energy of transfer is directly determined by the surface area of hydrocarbon in contact with water (38–40). Correspondingly, we find experimentally that the entropy for transfer of lipid monomers from water to micelles or membranes also depends linearly on the phospholipid hydrocarbon chain length (6):

$$\Delta S^e(T) = \left( \frac{\partial \Delta S^e(T)}{\partial n_{CH}} \right) \times n_{CH} + \Delta \Delta S^e(T). \quad (7)$$

From Eqs. 6 and 7, it therefore follows that the entropy of transfer is also linear with lipid chain length.
in agreement with experiment (8). Also, a linear dependence of the heat capacity for lipid monomer transfer from water to micelles/membranes is found experimentally (6):

\[ \Delta S^o_{\text{tr}}(T) = \left( \frac{\partial \Delta S^o_{\text{tr}}(T)}{\partial n_{\text{CH}}} \right) \times n_{\text{CH}} + \Delta \Delta S^o_{\text{tr}}(T), \]

with relatively little temperature dependence.

Because \( \Delta H^o_{\text{tr}}, \Delta S^o_{\text{tr}}, \) and \( \Delta C^o_{\text{tr}} \) depend linearly on chain length, both \( \Delta H^o_{\text{tr}} \) and \( \Delta S^o_{\text{tr}} \) must be linearly dependent on \( \Delta C^o_{\text{tr}} \), as given by Eqs. 1 and 2, respectively. Identifying the gradient of the transfer enthalpy with respect to \( \Delta C^o_{\text{tr}} \) in Eq. 7 with that in Eq. 1 requires the relation \( \frac{\partial \Delta H^o_{\text{tr}}(T)/\partial n_{\text{CH}}}{\partial \Delta C^o_{\text{tr}}(T)/\partial n_{\text{CH}}}(T-T^o_{\text{tr}}) \) between the chain-length dependences in Eqs. 7 and 9. If \( \Delta \Delta C^o_{\text{tr}} << \Delta C^o_{\text{tr}} \) in Eq. 9, then the constant term in Eq. 1 is given by \( \Delta H^o_{\text{tr}} \equiv \Delta H^o_{\text{tr}}(T^o_{\text{tr}}) \equiv \Delta H^o_{\text{tr}}(T^o_{\text{tr}}) \), which is independent of \( n_{\text{CH}} \). By an analogous procedure, we arrive at Eq. 2 for the entropy of transfer, where \( \Delta S^+ = \Delta \Delta S^o_{\text{tr}}(T^+_{\text{tr}}) \) is independent of \( n_{\text{CH}} \). Therefore, the condition for convergence is that the chain-length-dependent part of the heat capacity of transfer must be much larger than other contributions. For self-assembly of lipids, the dependence of \( \Delta C^o_{\text{tr}} \) on \( n_{\text{CH}} \) is dominated by the hydrophobic effect, which is characterized by a particularly high heat capacity, hence satisfying the condition for convergence.

We thus find that convergence for a given lipid type is linked to the linear dependence of the free energy and heat capacity of self-assembly on chain length. As is evident in Fig. 1, convergence is somewhat better within the lyso-phosphatidylcholine or diacyl-phosphatidylcholine data sets individually than between the two data sets. This suggests that slight differences in convergence temperature might also be expected between species with different head-groups. However, as seen already in Fig. 4, this discrepancy is compensated by using the effective heat capacity obtained from the measured CMCs with the definition given in Eq. 5. Note that the approach is rather general and might also work with surfactants. For instance, micelle formation by homologous alkyl glucosides (41), and alkyl dimethylphosphine oxides (42), appears to display approximate enthalpy convergence.

Similar principles should apply to the partitioning of amphiphiles into membranes. We expect an equation of state that has the same form as Eq. 3, but the effective heat capacity of transfer is given by replacing [CMC] with \( 1/K_p \) in Eq. 5, where \( K_p \) is the mole-fraction partition coefficient. The equation of state also contributes to the kinetics of monomer transfer from micelles or vesicles. For micellar self-assembly, the off-rate constant \( k_- \) is related to the on-rate constant \( k_+ \) by detailed balance (see, e.g., Cevc and Marsh (9)),

\[ k_- = k_+[\text{CMC}], \]

where [CMC] is expressed as a molar concentration when the units of \( k_+ \) are M\(^{-1}\) s\(^{-1}\). The activation energies \( E_{a-} \) and \( E_{a+} \) are therefore related by

\[ E_{a-} = E_{a+} - \Delta G^o_{\text{tr}}(T) + RT \ln(10^{3} k_{o-}/k_{o+}), \]

where \( \Delta G^o_{\text{tr}} \) given by Eq. 5 is the free energy for transfer from water to micelle, and the factor \( 10^{-3} \) m\(^3\) corrects the concentration units. The preexponential coefficients, \( k_{o-} \) and \( k_{o+} \), can be estimated by using Kramers’ theory (43), and by assuming a diffusion-controlled on-rate (15), respectively. We then get

\[ \ln(k_{o-}/k_{o+}) = \Delta S^o_{\text{tr}}/R - \ln(2\pi l_{c}\sigma_{\text{coll}}), \]

where \( l_{c} \) is the effective collision diameter, \( l_{b} \approx 0.07 \text{ nm} \) (44) is the width of the transition-state barrier for leaving the aggregate, and \( \Delta S^o_{\text{tr}} \) is the transition-state entropy.

Thermodynamics of the hydrophobic effect are characterized by an unusually large heat capacity (27). This is true also of phospholipid self-assembly, dealt with here, and the folding/unfolding of proteins (4). An inevitable consequence is that the enthalpy of transfer will go to zero at some particular temperature, as also will the entropy of transfer, although at a different temperature (cf. Figs. 3 and 4). Any claims for a nonclassical hydrophobic effect that are based on relative enthalpic and entropic contributions to the free energy at a fixed arbitrary temperature are therefore inappropriate. As seen in connection with Fig. 4, the enthalpy goes to zero and the transfer free energy becomes totally entropic at the special temperature \( T^o_{\text{tr}} - \Delta H^o_{\text{tr}}/\Delta C^o_{\text{tr}} \), which depends both on the lipid chain length and on the reference state chosen for the transfer process. The isentropic and isenthalpic temperatures nearly coincide using the limited data set for protein folding, but not for phospholipid self-assembly or simpler transfer processes that involve the hydrophobic effect (see Table 3). This probably has its origin in the difference in configurational entropy between lipid chains in a micelle and amino-acid side chains in the core of a globular protein. The high heat capacity also gives rise to considerable entropy-enthalpy compensation; this results in a relatively shallow temperature dependence of the CMC needed to achieve self-assembly, as is observed (see Fig. 4).

**APPENDIX: MICELLE-FORMING AND BILAYER-FORMING LIPIDS**

The treatment given in this article assumes that the self-assembled lipids are in thermodynamically equivalent states, independent of whether the aggregated state is a micelle or an extended bilayer. Which of the two types of aggregate forms, is determined by packing restrictions that depend on the lipid chain length. Fig. 7 shows the chain-length dependence of the transfer
FIGURE 7 Chain-length dependence of the standard free energy of transfer (see Eq. 4) of 1,2-diacyl phosphatidylcholines (n:n)PC from water to micelles (or bilayers) at 21–25°C. (Circles) All experimental data points collected in Marsh (8), which includes those in Table 1. (Solid line) Linear regression to all data points; (dashed line) linear regression for data with n ≤ 10. Uncertainty range without symbol is extrapolated to n = 12 from the linear regression.

free energy of 1,2-diacyl phosphatidylcholines (n:n)PC from monomers in water to the self-assembled state. The shorter-chain lipids (n = 5–8) form micelles, albeit of progressively increasing size, and the longer-chain lipids, n = 9–12, form bilayers (28,45). Nonetheless, there is a progressive increase in negative transfer free energy with increasing chain length. Buboltz and Feigenson (13) point out that the transfer free energy for n = 12 lies significantly below the linear extrapolation (dashed line) from the lipids with shorter chains, including those forming bilayers. The situation for the longest chains, n = 16, is somewhat uncertain because this involves an extrapolation from measurements in methanol-water mixtures (14).

The available data therefore suggest that, to lowest order, the lipids assembled in micelles and bilayers are in comparable states thermodynamically, but there may be differences in stability of the bilayer aggregates when the lipid chains become longer. Note that chain order in the liquid-crystalline bilayer state of diacyl phosphatidylcholines with different chain lengths is comparable when at the same temperature (46).

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