Direct observation of current in type I ELM filaments on ASDEX Upgrade

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Abstract

Magnetically confined plasmas are often subject to relaxation oscillations accompanied by large transport events. This is particularly the case for the high confinement regime of tokamaks where these events are termed edge localized modes (ELMs). Present ELM theories rely on a combined effect of edge current and the edge pressure gradients which result in intermediate mode number \( n \approx 10 - 15 \) structures (filaments) localized in the perpendicular plane and extended along the field lines. By detailed localized measurements of the magnetic field perturbation associated to type I ELM filaments it is shown that these filaments carry a substantial current.

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Edge localized modes (ELMs) are short (ms) breakdowns of the high confinement regime (H-mode), which is envisaged to be used in power producing tokamaks. Due to the high power fluxes, ELMs pose high demands on the plasma facing components, that are hard to meet. Thus better insight and control of ELM events is one of the foremost priorities in fusion research. Moreover the interest in ELM physics is enhanced by some fascinating analogies with sporadic explosive events as observed for example in solar flares [1] or in magnetic substorms [2].

At present ELMs are thought to originate from a combination of current and pressure gradient driven MHD modes [3], and result in a medium number ($n \approx 10 - 15$) of structures [4–7], localized in the perpendicular plane and extended along the magnetic field. These filaments travel through the Scrape Off Layer (SOL) and were measured by Langmuir probes on various machines, see e.g. [8], and observed by high speed cameras [7] or Gas Puff Imaging diagnostic [9].

Magnetic fluctuations associated with ELMs are usually believed to originate from MHD activity. Measurements of magnetic activity were previously performed by magnetic pickup coils close to the vessel wall [7, 10] or on insertable probes [11]. These measurements generally took place far from the filaments. This made it difficult to observe the magnetic perturbation of individual filaments and to examine the magnetic fine structure of the ELMs. Both would result in important information such as the excursion of magnetic field lines from their equilibrium position and if the ELMs are associated with reconnection events [1].

Here we report on measurements of type I ELMs carried out at ASDEX Upgrade (AUG) by means of a newly constructed probe head (more in [12]). The probe head consists of a cylindrical graphite case ($\varnothing = 60$ mm) which holds six graphite pins: one measured the ion saturation current, one was swept, whereas the others were floating. Inside the case, 20 mm behind the front side, a magnetic sensor with 1 MHz bandwidth, measured the time derivative of the three magnetic field components. A similar probe with combined electrostatic and magnetic signals was already used in AUG [11], but with a wider magnetic coil and a larger distance between electrostatic and magnetic sensors. Our probe was mounted on the midplane manipulator and inserted from the low field side for 100 ms 12 mm inside the limiter position. The data were obtained in type-I ELMy plasma discharges (# 23158,23159,23160,23161,23163) with a toroidal magnetic field of -2.5 T, 0.8 MA plasma current, $6.5 \times 10^{19}$ m$^{-3}$ central electron density and a $q_{95}$ value of 5.2.

We used the ion saturation current to infer the passage of a type-I ELM in front of the probe, as done in [13]. In analyzing ELM events we employ the idea that the magnetic signal during the ELM can be separated into different frequency components. We presume higher frequencies,
above few hundred kHz, to be generated mostly by Alfvénic activity or high frequency turbulence. These are not considered here, also because of the frequency cut-off by the graphite shield[12]. Additional MHD activity will still be present in the signal at frequencies below 20 kHz, but during ELM filaments most of the signal is presumed to originate from slowly varying currents convected with the filaments. This is justified by the so-called Degree of Polarization (DOP) analysis [14], which is a test for a plane wave ansatz, quantifying how well the relation $k \cdot B = 0$ is satisfied. It is based on the evaluation and diagonalization of the spectral matrix $S = \langle B_i^* B_j \rangle$, calculated in Fourier space. The DOP represents a measure to determine whether $S$ represents a pure state quantifying how well one single eigenvector approximates the state. A high DOP implies that the fluctuations are coherent over several wavelengths. Thus the method can be used to distinguish between propagating modes and coherent localized fluctuations. Fig. 1 (a), shows the results of DOP analysis as a function of frequency and time. The temporal evolution of the ion saturation current is depicted in the lower panel. A sudden drop in the DOP is observed corresponding to a steep increase of $I_{sat}$ signals: this implies that the magnetic field fluctuations during an ELM can better be represented by coherent structures than by plane wavepackets. A coherence analysis between the ion saturation current and the poloidal component of the magnetic field (Fig. 1 (c)) reveals an increase of coherence between the two signals during the ELM activity.

In Figure 2 (b), the increase of magnetic fluctuation amplitude is observed to be associated to a change of the phase relation of the radial and poloidal components ($b_r$ and $b_p$ ) as highlighted by the color box. In particular, the hodogram of the perpendicular magnetic perturbation (Fig. 2 (c)), i.e. the magnetic field perturbation trajectory in the $b_r - b_p$ plane, during the passing of the ELM, exhibits a closed orbit at the time interval marked in Figure 2 b, which is compatible with the passing of current filaments in front of the probe. Outside the ELM the magnetic field perturbation exhibits an almost linear polarization in the perpendicular plane. This shows clearly that magnetic activity in between ELMs (wavelike) differs qualitatively from the magnetic perturbation during an ELM, which seems to be due to the motion of current filaments.

Measuring all three components of the magnetic perturbation allows checking the alignment of the current filaments directly. In Fig. 3 (a) the trajectory of the magnetic field excursion during an ELM event in all three magnetic field components is shown. The time interval selected corresponds to the highlighted one in Fig. 2. A closed elliptical loop lying in a plane slightly tilted with respect to the local frame of reference is observed, as expected for filamentary structures. The direction normal to this plane is determine using the minimum variance analysis [15]. The method is based
on the solution of the eigenvalue problem $\sum_{\nu=1}^{3} M_{\mu \nu}^B n_{\nu} = \lambda n_{\mu}$ where $M_{\mu \nu}^B = \langle B_{\mu} B_{\nu} \rangle - \langle B_{\mu} \rangle \langle B_{\nu} \rangle$ is the Magnetic Variance Matrix, the brackets indicating the mean values averaged over the time the structure spends traveling in front of the probe, $\mu, \nu = 1, 2, 3$ denoting the cartesian components of $X, Y$ and $Z$ of the system, $\lambda$ and $n$ being the eigenvalues and eigenvectors of the system, respectively. The eigenvectors corresponding to the eigenvalues $\lambda_1$, $\lambda_2$ and $\lambda_3$, represent the direction of maximum, intermediate and minimum variance of the magnetic field respectively. The eigenvector $n_3$ corresponds to the direction of minimum variance and is normal to the plane spanned by the magnetic field perturbation. This direction is observed to be parallel to that of the equilibrium magnetic field (same figure blue line). This confirms the hypothesis that the ELM filament is aligned with the equilibrium magnetic field. From the sense of polarization the direction of the current is found to be colinear with the plasma current. The method allows the determination of the rotation matrix, so that the hodogram in the plane perpendicular to the current filaments may be reconstructed. This hodogram is shown in Fig. 3 (b) together with a fit to an ellipse. The shape of the hodogram calculated in the rotated frame of reference can be used to determine the type of current distribution associated to an ELM. Theories proposed ELM filaments to be associated to monopolar [4, 16] or to bipolar current distributions [17]. Up to now no clear evidence of one mechanism predominant with respect to the other was reported. Fig. 3 (c) shows the anticipated shape of the hodogram in bipolar and monopolar cases. In a bipolar case the hodogram exhibits a cardioid-like shape with a cusp at the origin representing a distinct signature. This cannot be recognized in the experimental data (see Fig 3 (b)). To reinforce the statement we note that a bipolar-like hodogram with the presence of a cusp was previously recognized in [18] (cfr. Fig 3(b)) where it was associated to a direct measurement of a bipolar current. We emphasize, however, that the filaments observed in [18] are of completely different origin as induced by drift-Alfvén turbulence [19]. A further corroboration of the hypothesis of monopolar current filaments is yielded by the quadrants covered by the magnetic field trajectory. While a monopolar current hodogram regularly occupies two quadrants, the bipolar one always spans three quadrants: this latter behavior is not observed in the experimental data as can be verified by comparing Fig. 3 (b) and Fig. 3 (c). These results make us confident that the magnetic fluctuations observed are indeed generated by a monopolar current distribution. Under this basic assumption the current carried by this filament may be estimated. In the rotated frame of reference for a circular monopolar symmetric filament drifting in the $\lambda_1$ direction, the two perpendicular magnetic field components may be written as
\[ b_{\lambda_1} = -\frac{r_0 B_0 a}{\lambda_1^2 + a^2} \text{ and } b_{\lambda_2} = -\frac{r_0 B_0 a}{\lambda_2^2 + a^2} \] where \( B_0 = \frac{\mu_0 I_0}{2\pi r_0} \) and \( a \) is the distance between the filaments center and the probe, representing also the distance of closest approach, \( r_0 \) is the filament radius and \( I_0 \) its current. The distance \( a \) can be approximated, assuming the filament to propagate with a constant velocity in the \( \lambda_1 \) direction: \( a = \Delta t v_{\lambda_1} \) where \( \Delta t \) is the time delay between the maximum of \( b_{\lambda_1} \) and the maximum/minimum of \( b_{\lambda_2} \), where \( b_{\lambda_1} \) and \( b_{\lambda_2} \) are the projections of the magnetic field in the maximum-intermediate variance plane. Thus within these approximations the current may be estimated noting that \( |b_{\lambda_2}(\lambda_1 = a)| = \frac{\mu_0 I_0}{2\pi a} = \frac{\mu_0 I_0}{4\pi \Delta t v_{\lambda_1}} \). Applied to the experimental data, this computation is equivalent to calculating the quantities depicted in Fig. 4, where \( \Delta t \) was calculated both at the maximum and minimum of \( b_{\lambda_2} \). The two values \( \Delta t_1 \) and \( \Delta t_2 \) are equal to 38 \( \mu s \) and 42 \( \mu s \) respectively. The estimate of the current relies on the knowledge of the local velocity in the \( \lambda_1 \) direction. This propagation was reported for ASDEX Upgrade, e.g. [11, 20]. The experimental setup does not allow a reliable local measurements of \( v_r \) or \( v_p \), neither can we rely in the presented shots on correlation analysis of wall mounted probes (which are 160 degrees separated from the manipulator in the toroidal direction). Most likely these signals are indeed dominated by MHD mode activity in the confined plasma rather than current filaments in the SOL. As best approximation for radial propagation we thus assume the most probable value \( v_r = 1.2 \text{ km/s} \) as determined in [20] and calculate \( v_{\lambda_1} = v_r / \cos(\angle(\lambda_1 - r)) \), where \( \angle(\lambda_1 - r) \) is the angle between \( \lambda_1 \) and the radial direction which for the present case is of the order of 7\(^\circ\). From [20] we also estimate a standard deviation of \( v_r \) as \( \sigma_{v_r} = 700 \text{ m/s} \), which ensures that 71\% of the events are observed within \( (v_r \pm \sigma_{v_r}) \). With these values the average distance of closest approach is approximately 4 cm, and using the average value between the minimum and maximum of \( b_{\lambda_2} \) we obtain an estimate of 1.9 kA. The total perpendicular field \( \sqrt{b_{\lambda_1}^2 + b_{\lambda_2}^2} \) is shown in Fig. 4 (b). The magnetic field variation can be fitted by a function of the form \( f = \left( \frac{\alpha}{\sqrt{(t-t_0)^2 + \beta}} - \gamma \right) e^{-(t-t_0)/\tau_e}, t_0 \) being the time instant of the maximum of the total perpendicular field and \( \tau_e \) the \( e \)-folding time, and assuming the magnetic field to be the response of a passing monopolar current filament. The good quality of the fit provides additional support for the monopolar nature of the filament, also compared with the fit expected from a bipolar current distribution shown in blue line exhibiting an higher \( \chi^2 \). The average decay time is determined as \( \tau_e \approx 200 \mu s \). In order to increase the statistic reliability of the previous estimate we have analyzed events from 5 different shots with similar conditions. The results are shown in Fig. 5. In panel (a) the joint PDF of the independent experimental values \( \Delta t \) and \( b_{\lambda_2} \), used for the current evaluation, is shown, highlighting how the bulk of the filaments

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have values of approximately 25 µs and 5 mT. In panel (b) the histogram of the angle between \( \lambda_1 \) and the radial direction is shown, showing that the \( \lambda_1 \) direction is a complex combination of radial and poloidal propagation. Finally in panel (c) the current estimated according to the aforementioned formula is plotted vs the position of the filaments with respect to the separatrix, taking into account the position of the manipulator and the estimated distance of closest approach. The errors represent the influence of the velocity uncertainty on the estimates of \( a \) and consequently on \( I \). The bulk of the distribution of these filaments are thus observed in the SOL, even taking into account the uncertainty on \( v_r \); the median of the distribution of the filaments in the SOL within the error in their position is 1.4 kA, corresponding to a \( j_{||} \approx 4.5MA/m^2 \) for 1 cm radius filaments. These values are consistent with measurements of edge currents as seen e.g. in [21]. It was already supposed in [22] that, in case ELM breakdown is driven by peeling instabilities, this will lead to a flattening of the current density profile over the separatrix and an increase of currents flowing into the SOL. These currents will be nearly force-free and accompanied by poloidal halo currents closing through the divertor tiles. Actually these currents were measured [12, 23] with values up to few tens of kA, supporting the presence of rapid flow of toroidal currents from the plasma into the SOL. The resulting histogram may also be compared with the estimate for ELM filaments in JET given in [24]: in this case the most probable current was of the order of 450 A, but with a lower radial velocity postulated. For completeness it must be noted that the same current density was estimated in [11], assuming the magnetic perturbation to be induced by a rotating helical structure with a bi-directional current close to, but still inside, the separatrix. The value found is higher than the measured \( j_{sat} \) current density to the ion-biased pin (\( \approx 50 \) kA/m\(^2\)). Concluding this letter, we have provided evidence that ELM filaments carry considerable currents for which we found a reasonable estimates. The magnetic signals during ELM filaments differ substantially from wave activity in between ELMs. We have shown that the current in the filaments is co-aligned to the plasma current and of the magnitude expected for the edge. The current flows along the unperturbed magnetic field lines and has a unidirectional nature. This poses the question where the filament currents close in the SOL and why such high current densities are sustained in the ELM filaments. We hope that future experiments will contribute to answer these questions, which will throw new light on the instability mechanisms for ELMs.

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FIG. 1. Top: Degree of Polarization (DOP) as a function of time and frequency. Bottom: Ion saturation current ($I_{sat}$). Right: Coherence between $I_{sat}$ and $b_p$ computed in ELM and inter-ELM phases. The time intervals are shown in the bottom panel by colored boxes.
FIG. 2. (a) Ion saturation current (b) Poloidal and radial components of the magnetic field. Red box highlights the time interval when the two components change their phase relation. (c) Hodogram of radial/poloidal magnetic field components. Closed loop in red refers to time intervals highlighted in panel b.

FIG. 3. (a) Trajectory of ELM filament associated magnetic field excursions in all three spatial directions. Direction of minimum variance is shown (black line) together with direction of equilibrium field (dashed blue line). (b) Hodogram of magnetic perturbation associated with ELM current filament reconstructed in the maximum variance plane. Dashed red line shows the elliptical fit. (c) Hodograms calculated for a monopolar current distribution ($M$) and bipolar one ($B$).
FIG. 4. (a) Time traces of the two perpendicular components of magnetic field during an ELM filament. (b) Total perpendicular magnetic field as function of time. Superimposed results of a fit for an expected monopolar (red) and bipolar (blue) current distribution both modulated by an exponential decay.

\[ (b_1^2 + b_2^2)^{1/2} \]

\[ \chi^2_{\text{Monopolar}} = 1.51 \times 10^{-10}. \]

\[ \chi^2_{\text{Bipolar}} = 3.38 \times 10^{-10}. \]
FIG. 5. (a) Joint PDF of $\Delta t$ and $b_x(\lambda_1 = a)$ (b) Histogram of the angle between $\lambda_1$ and the radial direction. (c) Filaments current estimate vs distance from the separatrix estimated with $v_r = 1.2$ km/s. Error bars results from propagation of velocity uncertainty in the estimate of $a$ and $I$. 